

# How do aberration correctors work?

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CEOS

Corrected Electron Optical  
Systems GmbH



# Invention of the Transmission Electron Microscope

CEOS

Corrected Electron Optical  
Systems GmbH

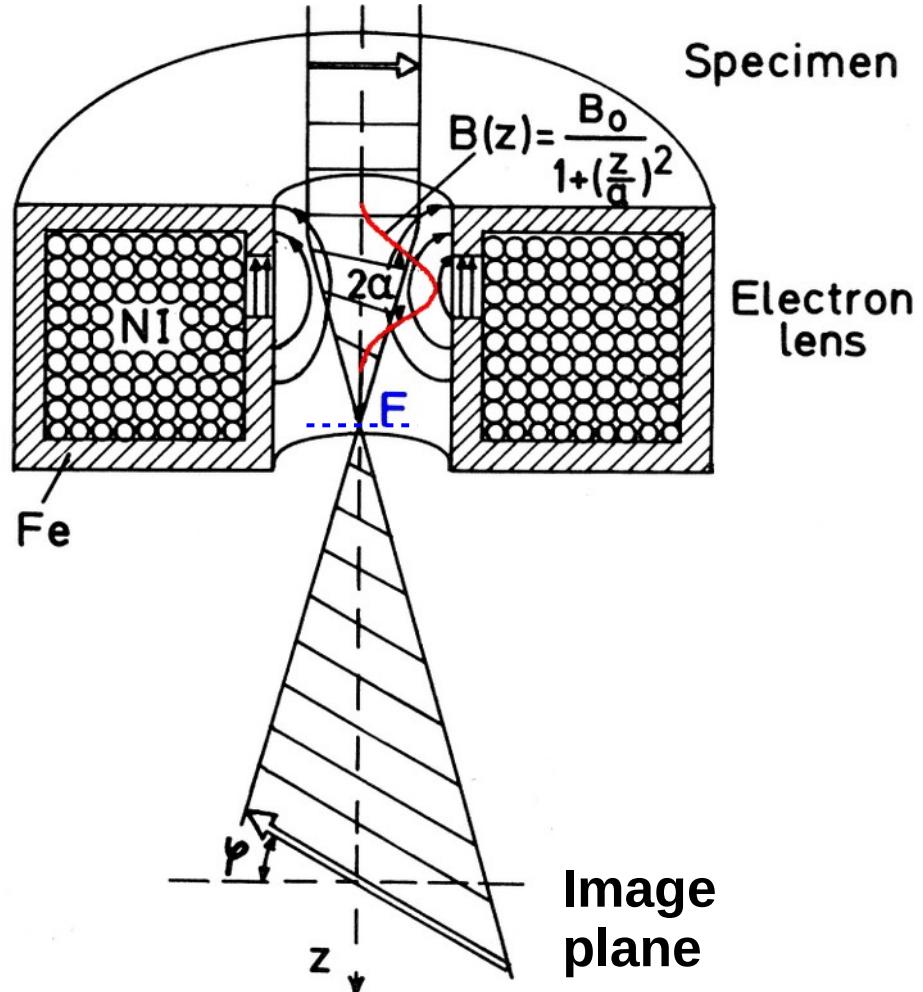


1931, TU Berlin



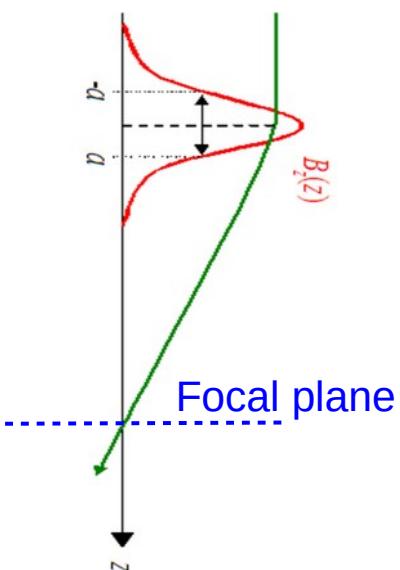


# Magnetic Lens for Electrons



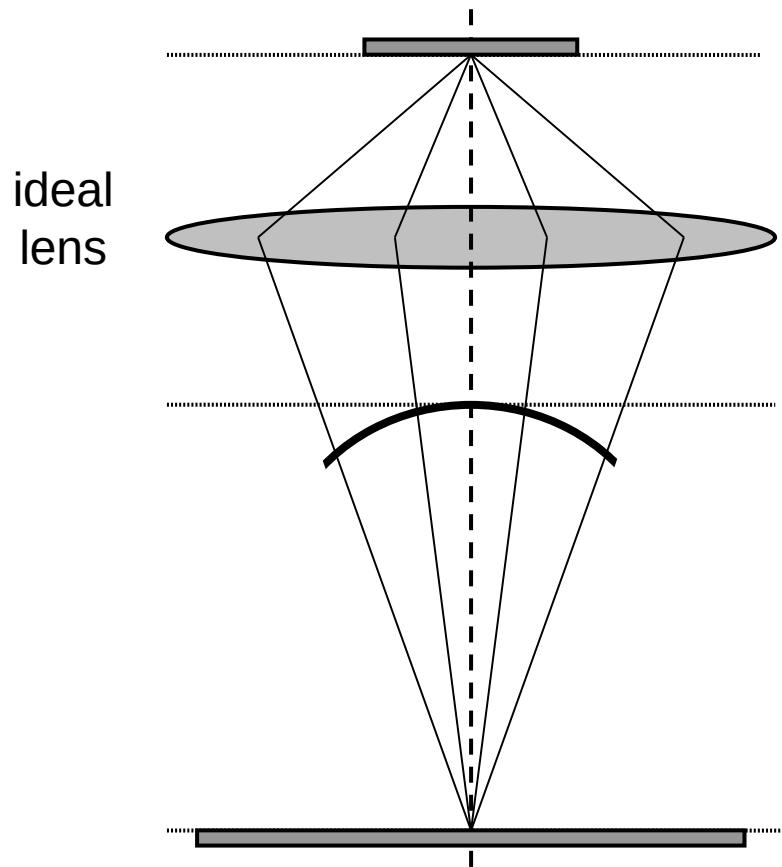
## Glaser's "Glockenfeld"

bell-shaped,  
axial magnetic field



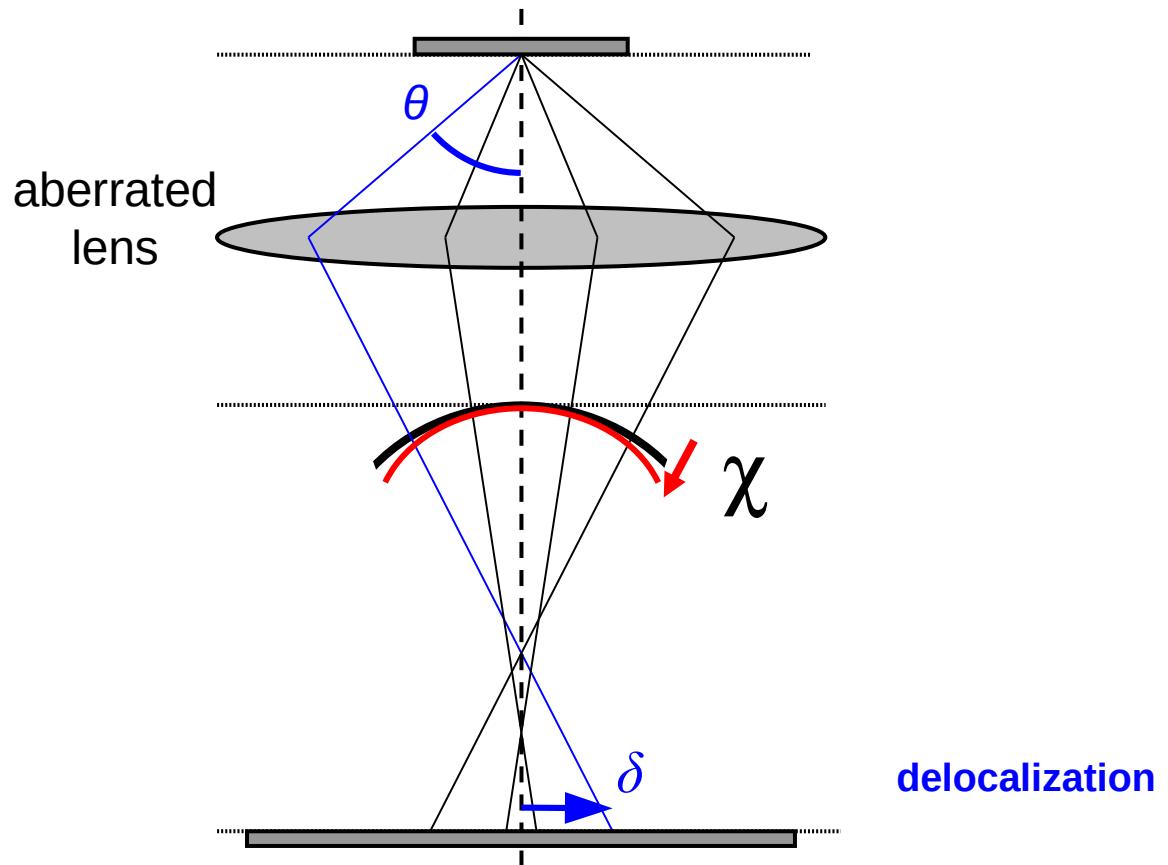


# Lens aberrations





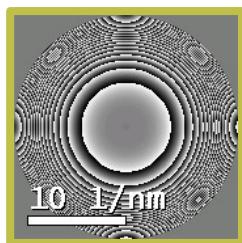
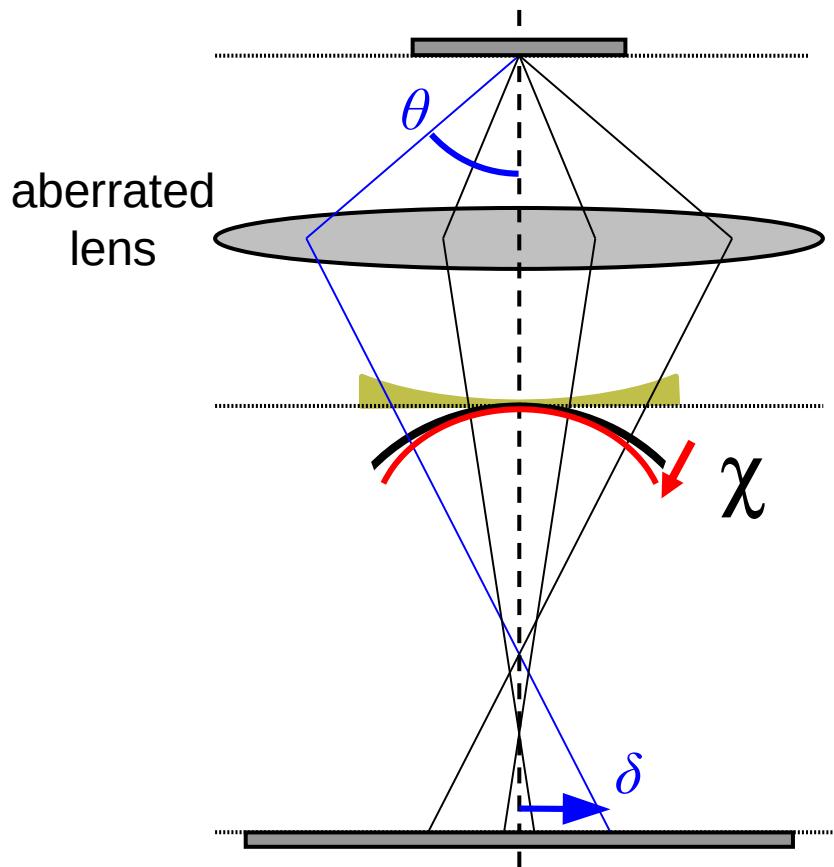
# Lens aberrations: Spherical aberration



delocalization

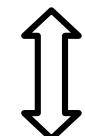


# Lens aberrations: Spherical aberration



phase plate

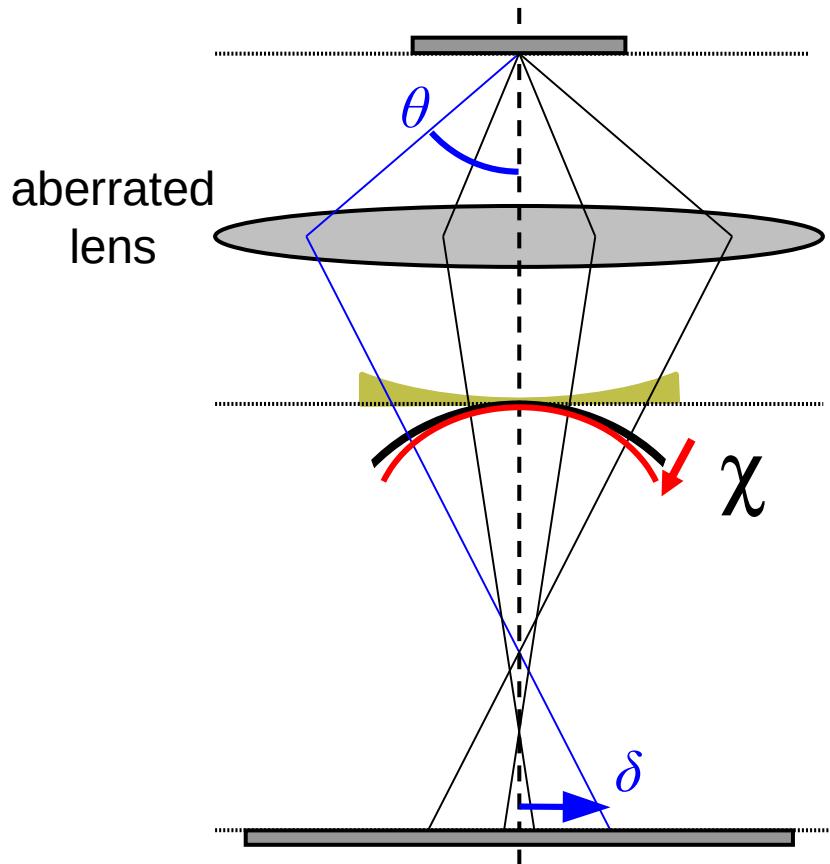
$$\exp\{-i\chi\} \quad \text{with} \quad \chi = \frac{2\pi}{\lambda} \cdot \frac{C_3}{4} \theta^4$$



$$\text{delocalization: } \delta = \frac{\nabla \chi}{2\pi} = C_3 \cdot \theta^3$$



# Spherical aberration : Scherzer's Theorem

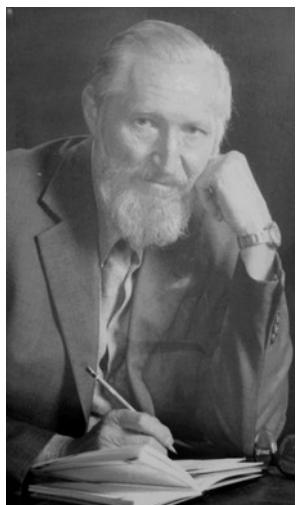


## Über einige Fehler von Elektronenlinsen.

Von O. Scherzer in Darmstadt.

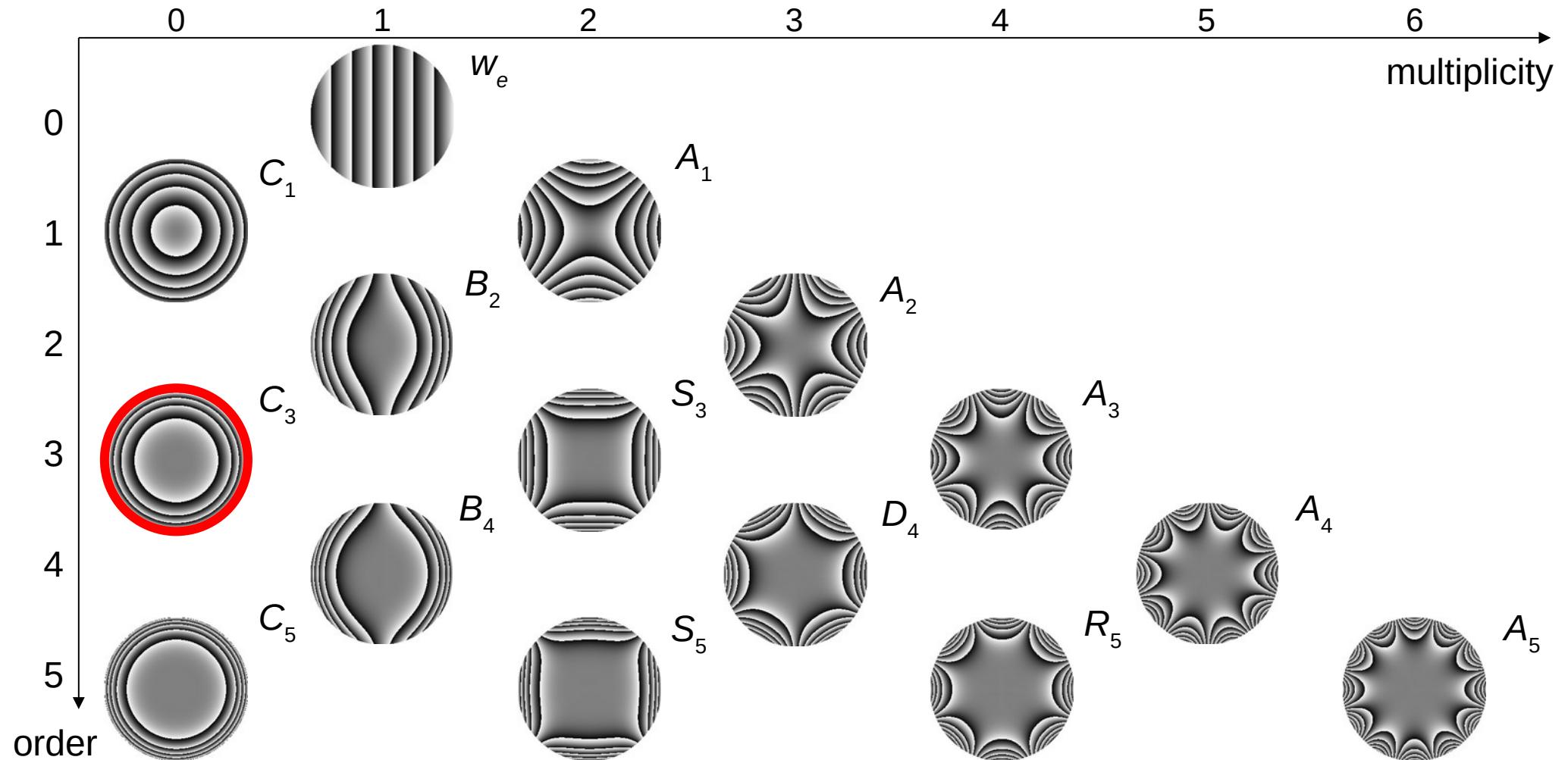
Mit 3 Abbildungen. (Eingegangen am 4. Juni 1936.)

Unmöglichkeit des Achromaten. Die Bildfehler dritter Ordnung. Unvermeidbarkeit der sphärischen Aberration.



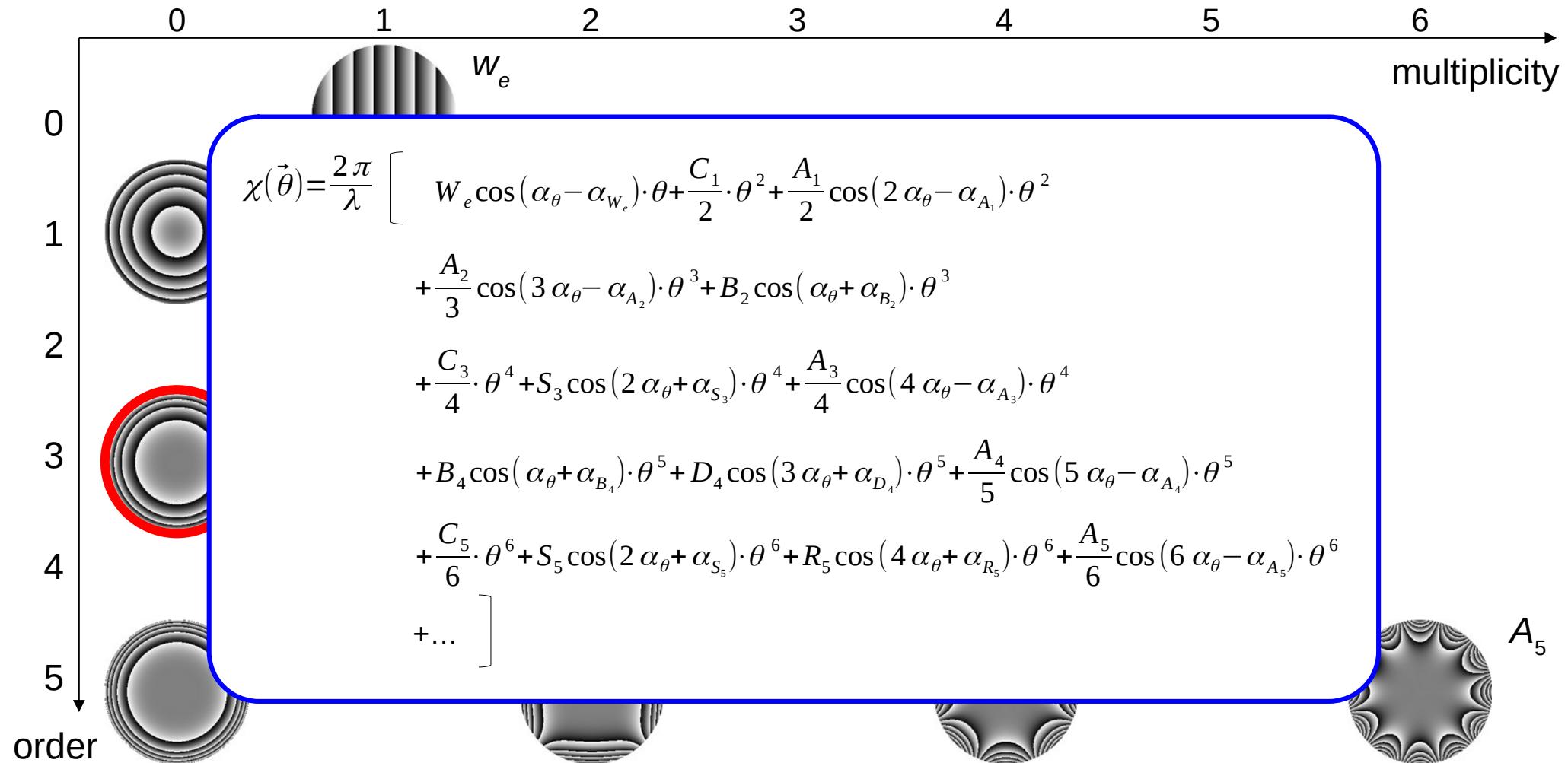
**Unavoidable positive spherical aberration for stationary, space-charge-free, round electron lenses!**

Prof. Otto Scherzer  
(TU Darmstadt)

Wave aberration  $\chi$ 

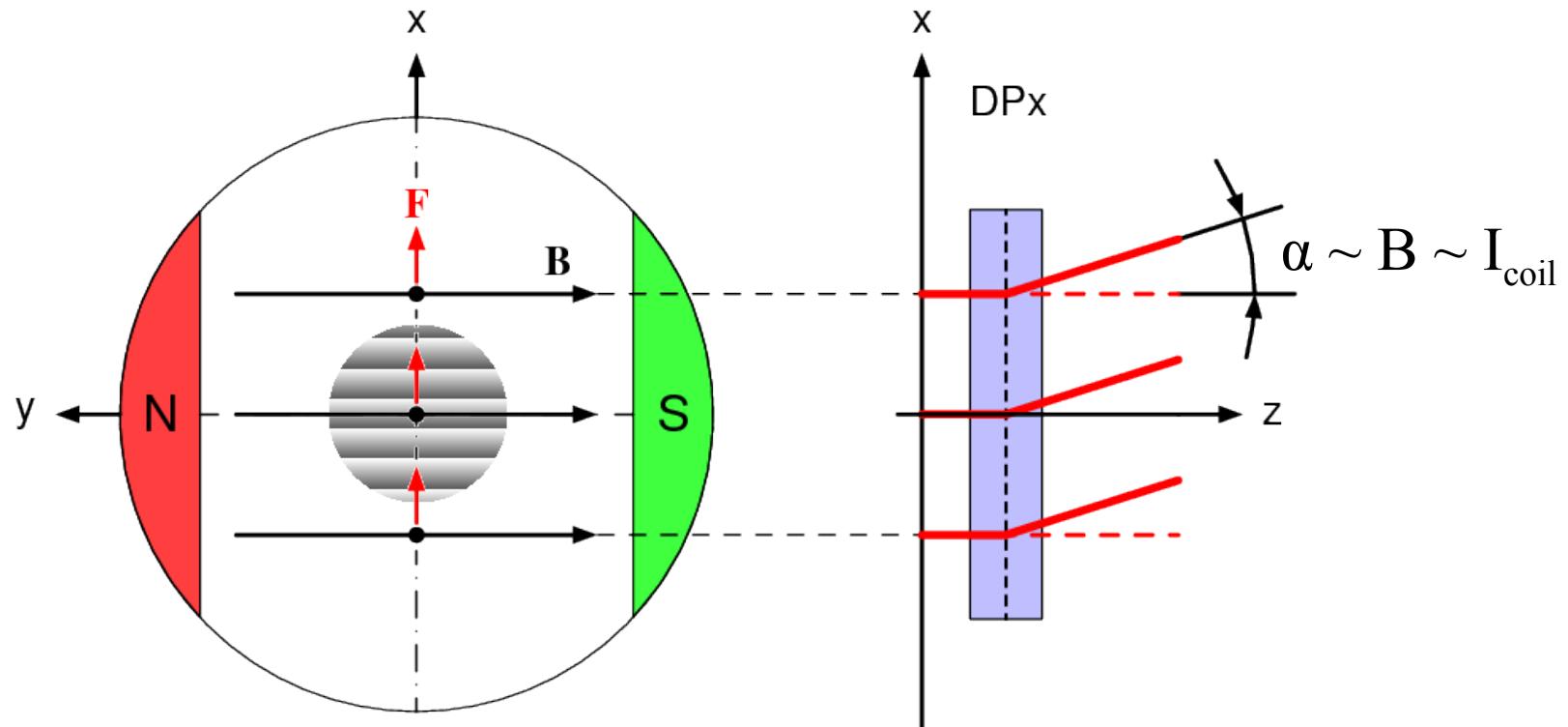


# Wave aberration $\chi$



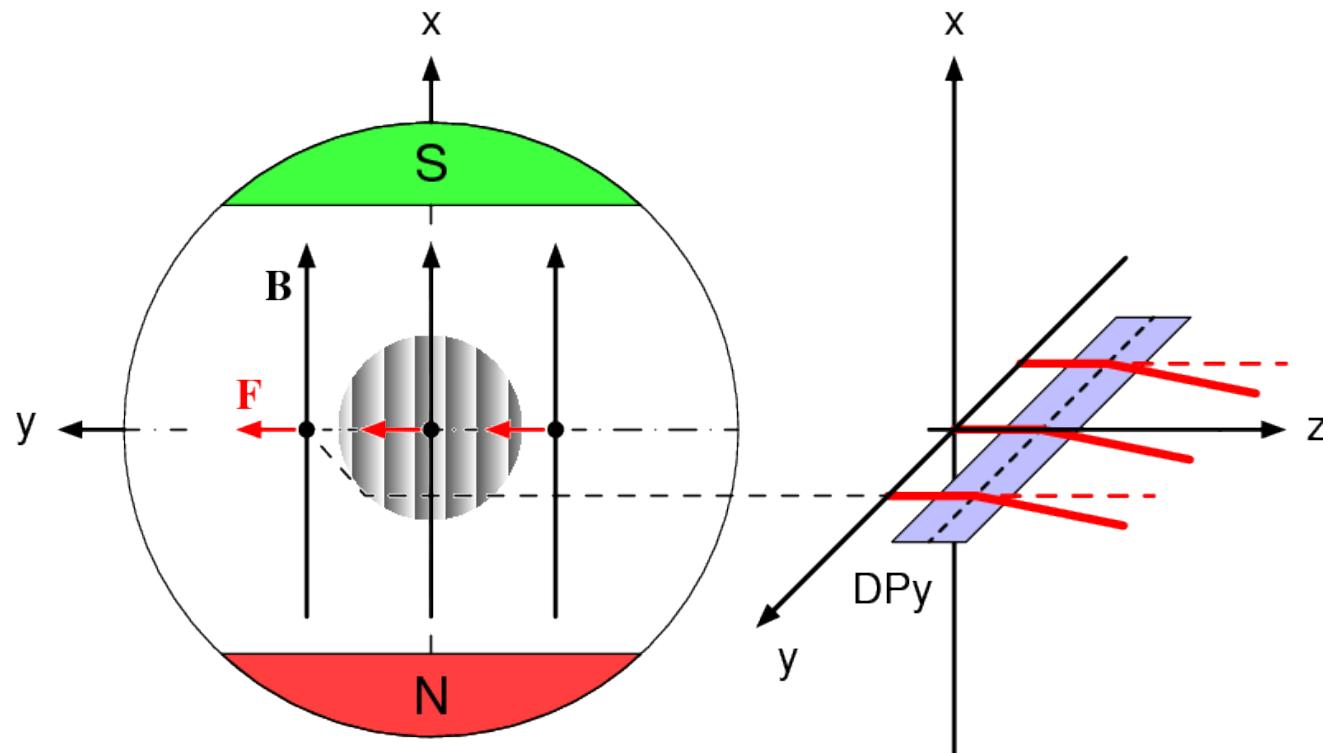


## Dipoles – beam deflection in x-section



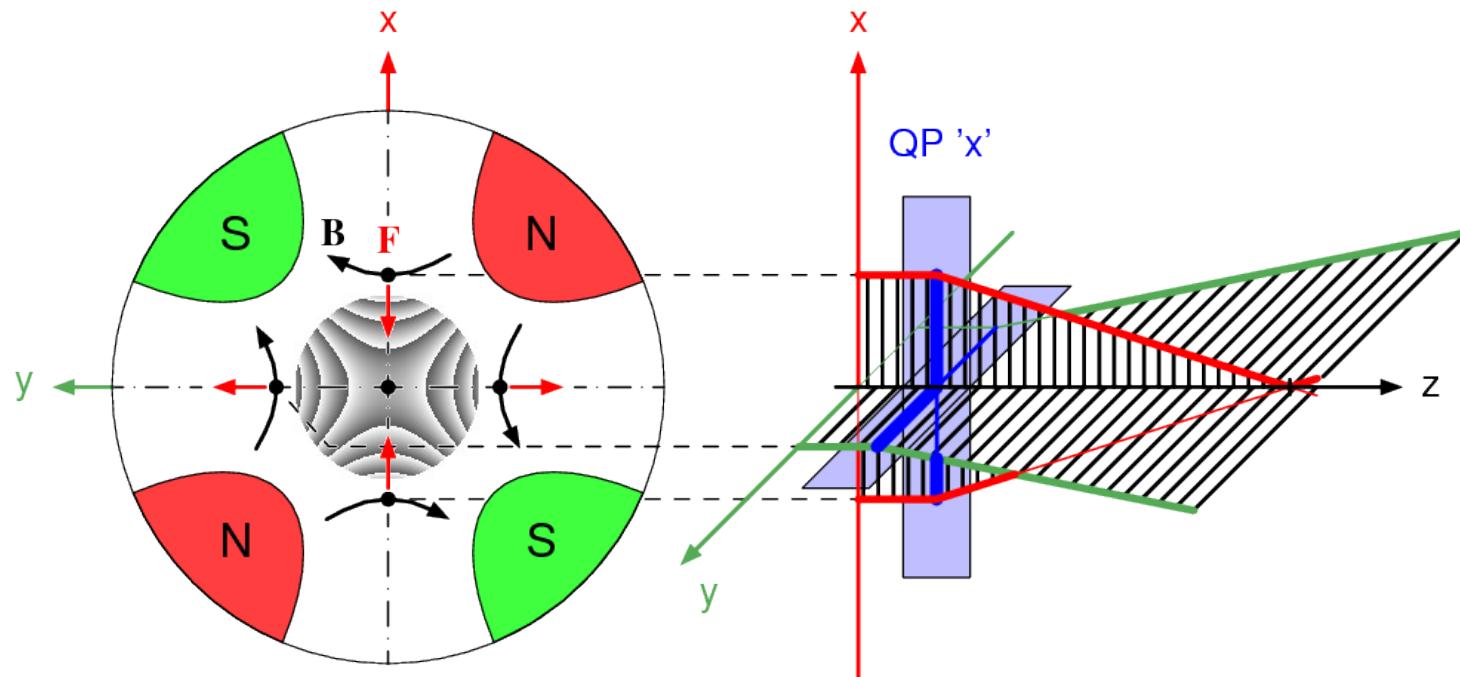


## Dipoles – beam deflection in y-section



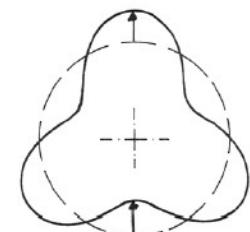
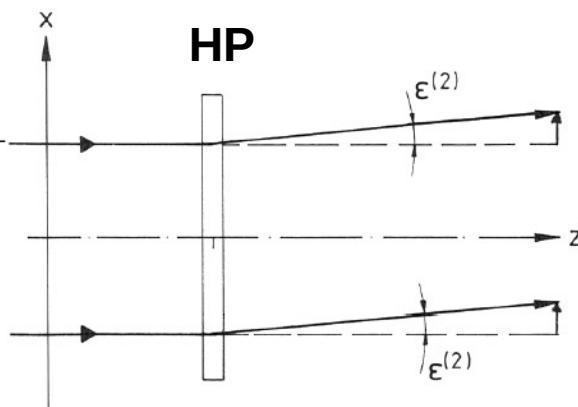
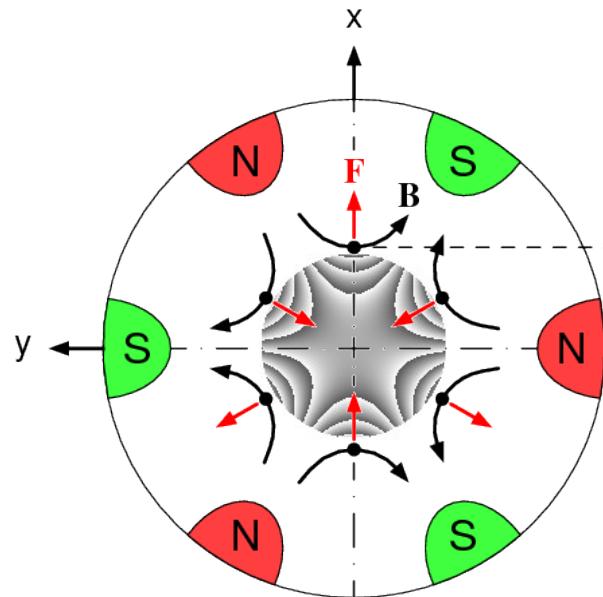


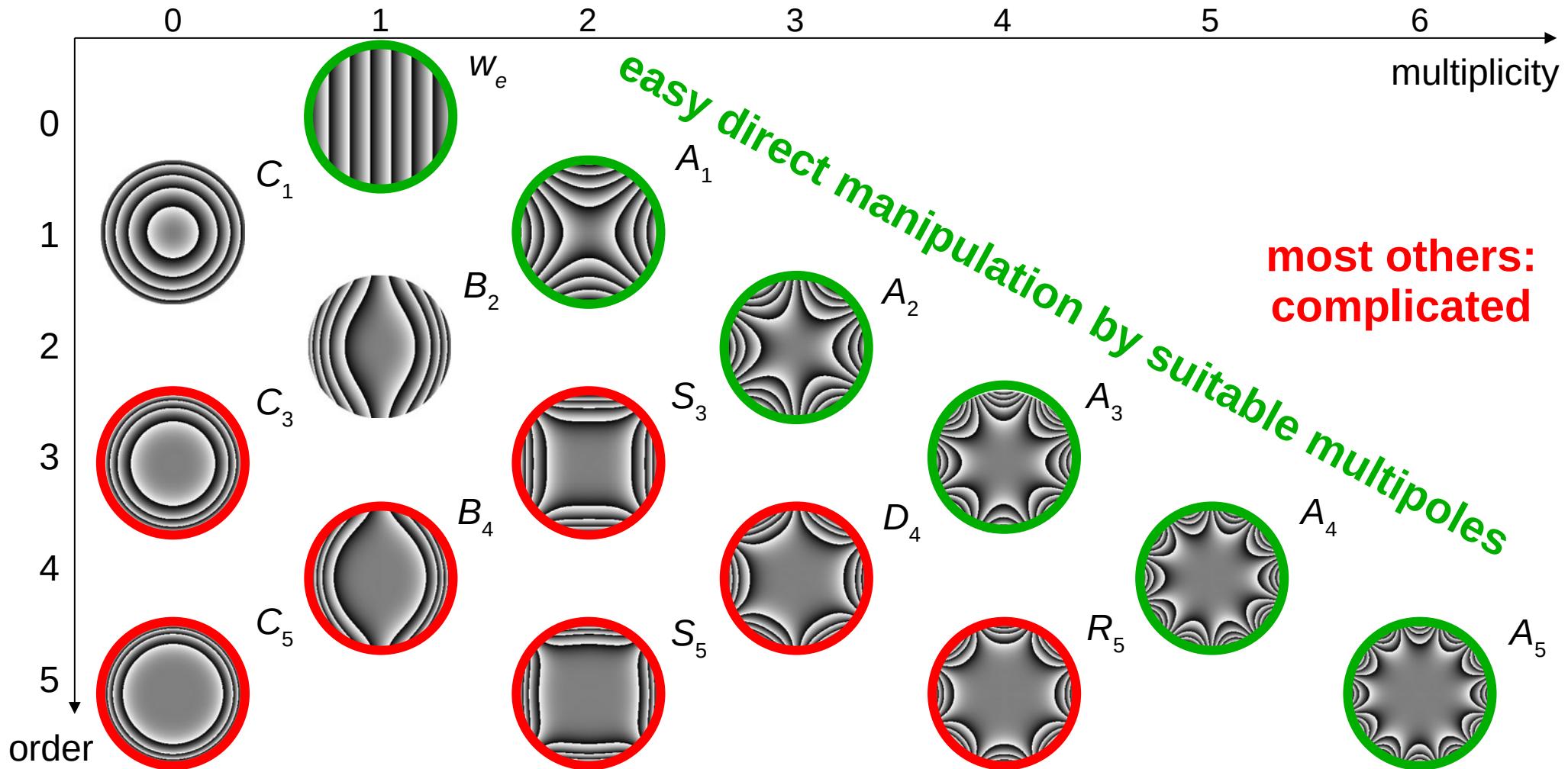
## Quadrupoles – 2-fold Stigmators





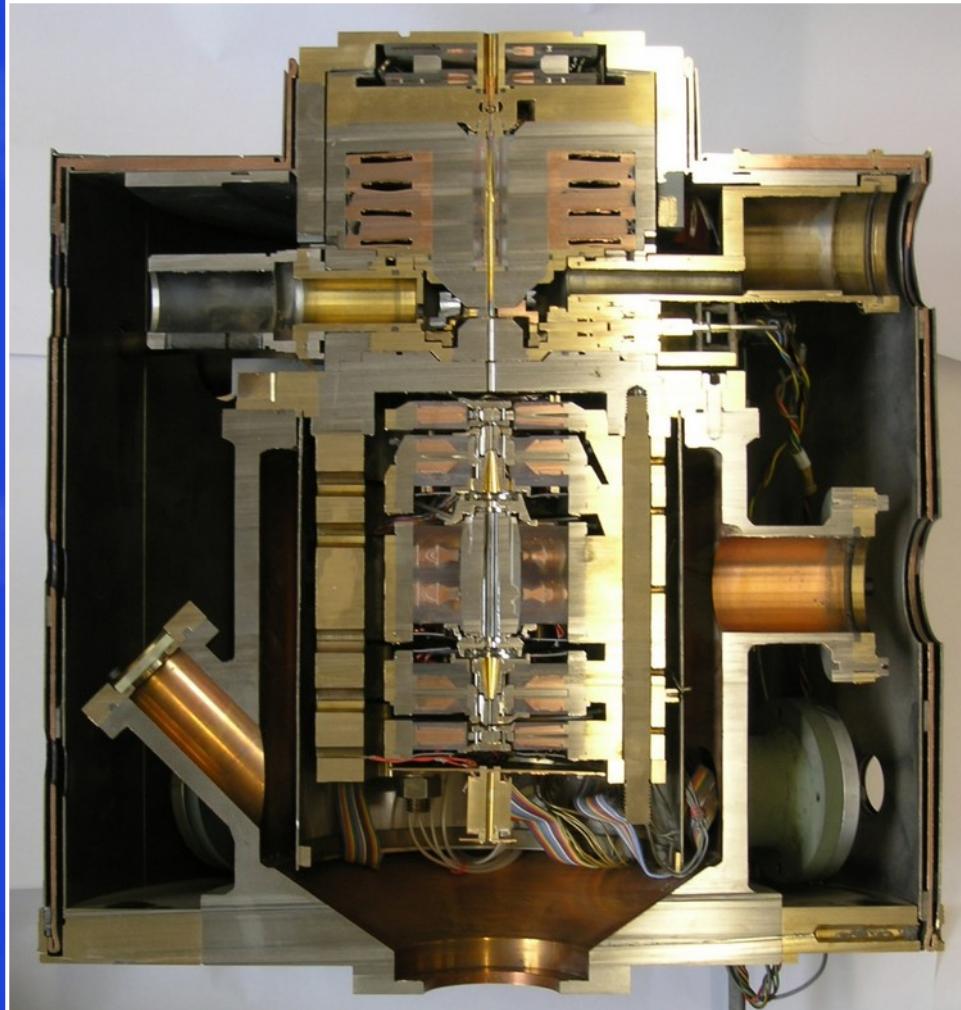
## Hexapoles – 3-fold Stigmators



Wave aberration  $\chi$ 



# Long history of aberration correction



## Darmstadt 1980 $C_c$ - $C_s$ -corrector Scherzer & Rose

Aberration correction was successfully shown in principle but did not improve the image resolution of the electron microscope.

- lack of precision machining
- lack of stability
- lack of aberration measurement
- ...

→ **No more funding ...**

same outcome world-wide  
e.g. in Chicago and Cambridge

# Aberration correction using hexapoles



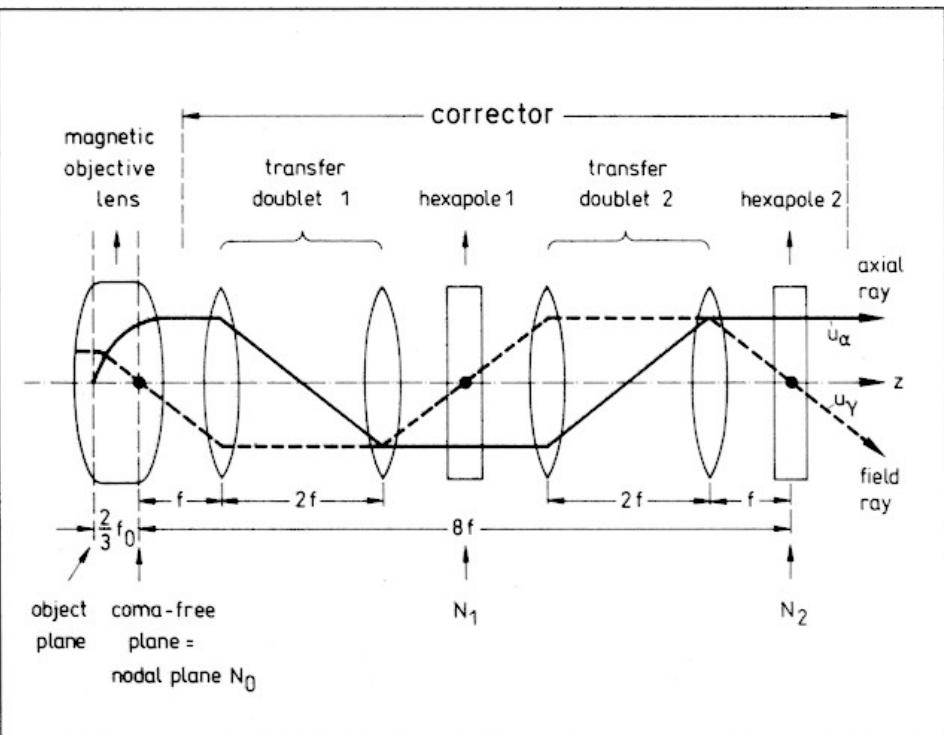
## Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG

**Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope.** A spherically corrected semiaplanatic objective lens for a subangstrom medium-voltage transmission electron microscope (TEM) is outlined. The aplanatic corrector consists of two telescopic round-lens doublets and two sextupoles centered about the nodal points of the second doublet. If the corrector is incorporated into a 300 kV TEM equipped with a field emission gun a resolution limit of 0.6 Å and  $10^4$  equally-well-resolved image points per diameter can be obtained. For achieving this performance the magnetic field of the objective lens must be stabilized with a relative accuracy of 1 ppm, while the fields of the corrector elements require at most a stability of 10 ppm.

**Entwurf eines sphärisch korrigierten semiaplanatischen Mittelspannungs-Elektronenmikroskops.** Eine in dritter Ordnung sphärisch korrigierte rein magnetische Objektivlinse, deren isotrope Koma beseitigt ist, wird vorgeschlagen. Das korrigierte Objektiv besteht aus einer Objektivlinse, zwei teleskopischen Rundlinsen-Doublets und zwei Sextupolen, deren Mitten in den Knotenebenen des zweiten Doublets liegen. Falls der Korrektor in ein 300 kV Transmissions-Elektronenmikroskop eingebaut wird, das mit einer Feldemissionskathode ausgestattet ist, können  $10^4$  Bildpunkte pro Durchmesser mit einer Auflösungsgrenze von 0.6 Å gleich gut aufgelöst werden. Um eine solche Auflösung zu erzielen, müssen die Beschleunigungsspannung und das Magnetfeld der zu korrigierenden Objektivlinse auf 1 ppm stabil gehalten werden. Für die Felder der Korrektorelemente genügt dagegen eine Stabilität von 10 ppm.



**Fig. 2. Schematic arrangement of the elements of the spherically corrected semiaplanatic objective lens.**



# Aberration correction by means of hexapoles

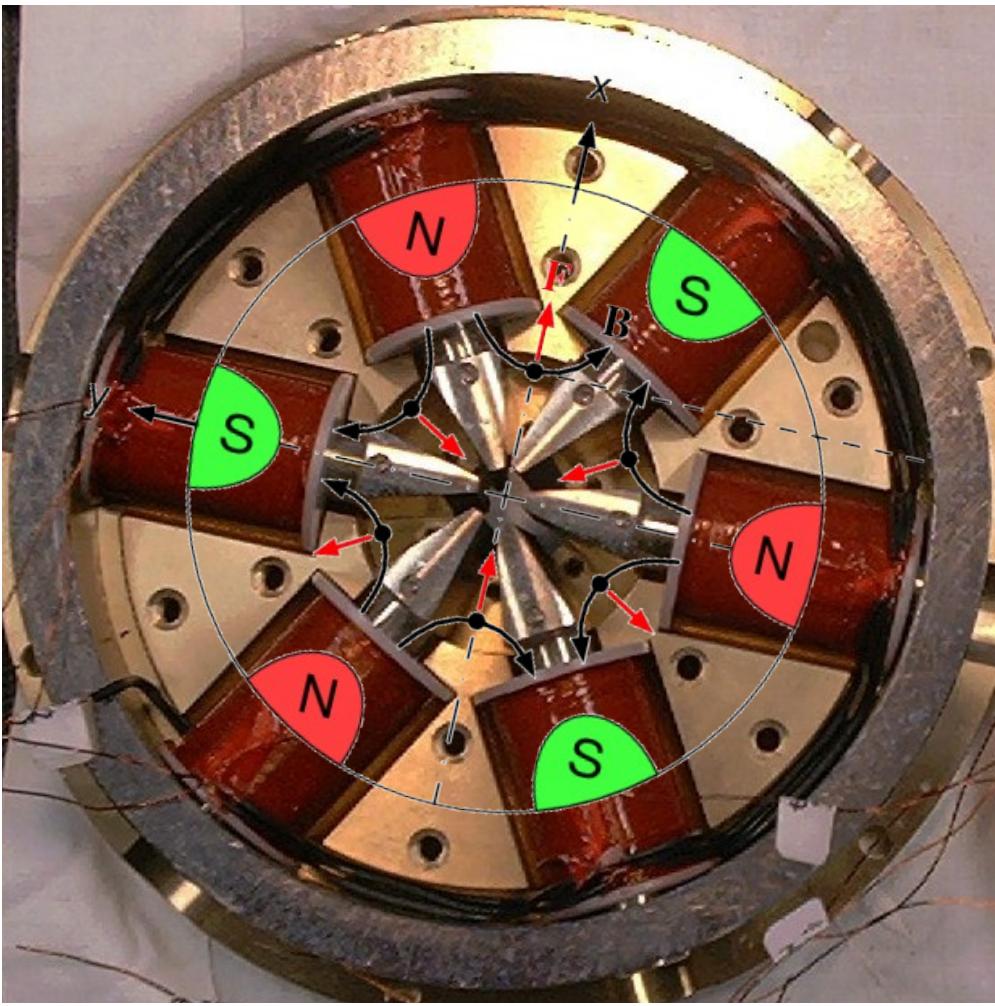
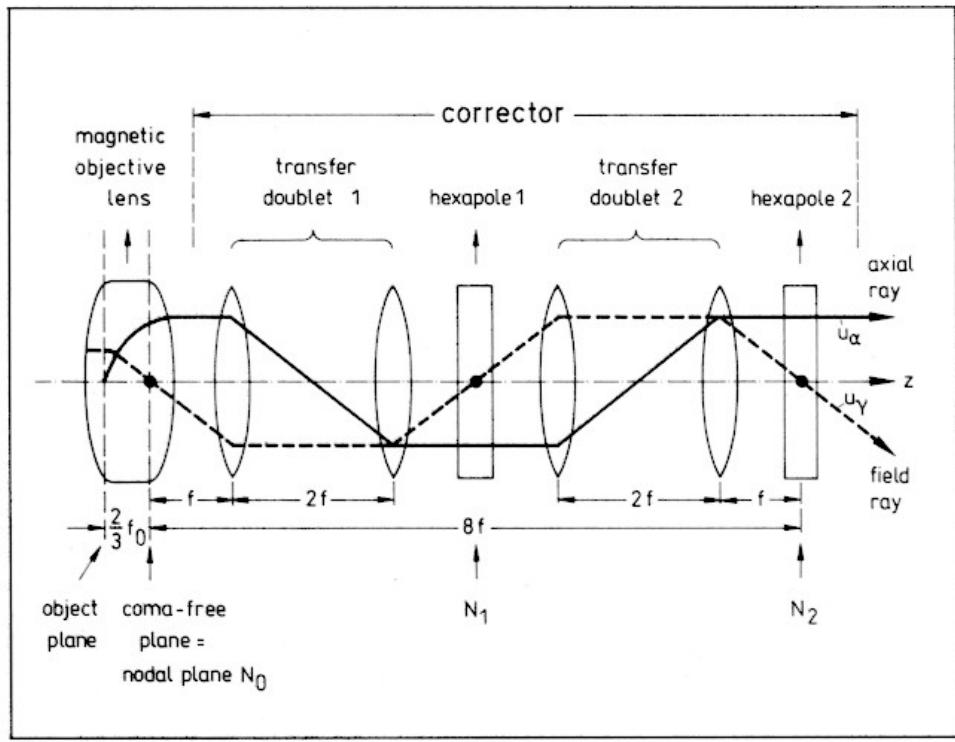
Optik

85, No. 1 (1990) 19–24 © Wissenschaftliche Verlagsgesellschaft mbH, Stuttgart

## Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

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# Aberration correction by means of hexapoles

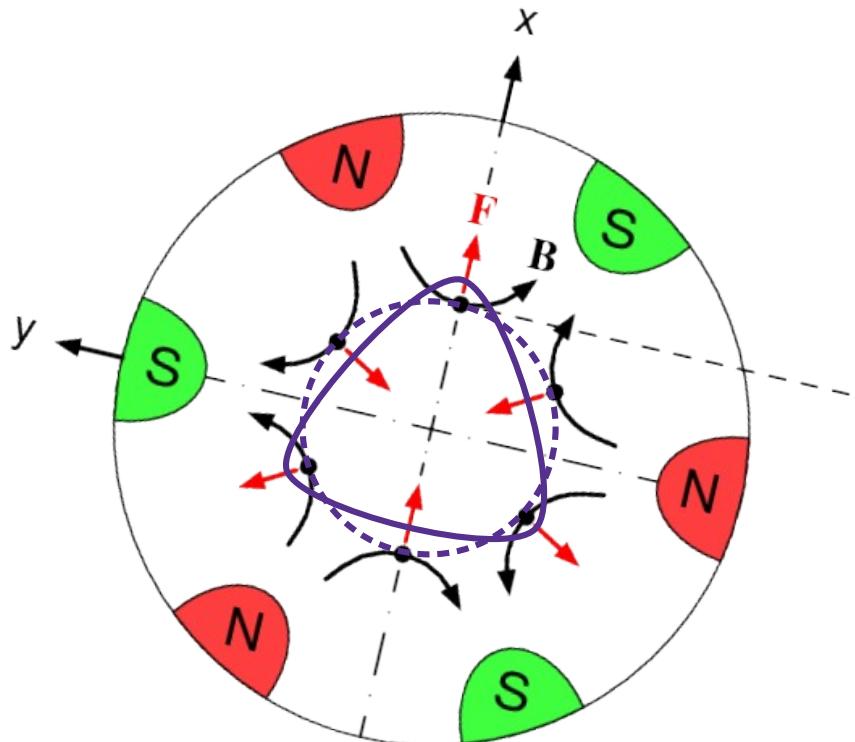
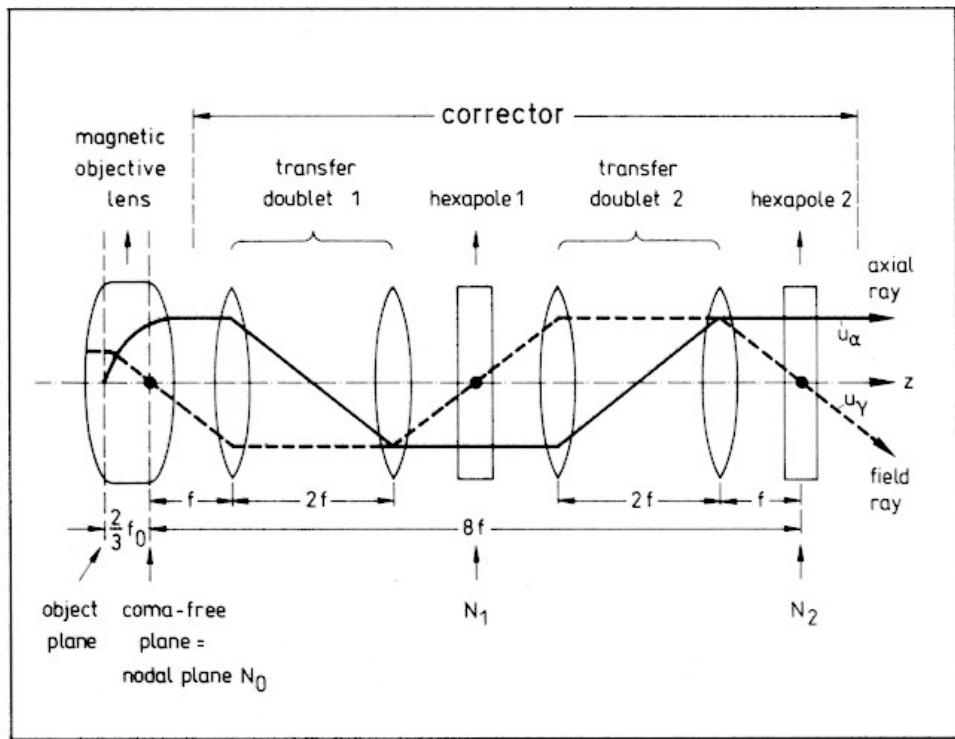
Optik

85, No. 1 (1990) 19–24 © Wissenschaftliche Verlagsgesellschaft mbH, Stuttgart

## Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

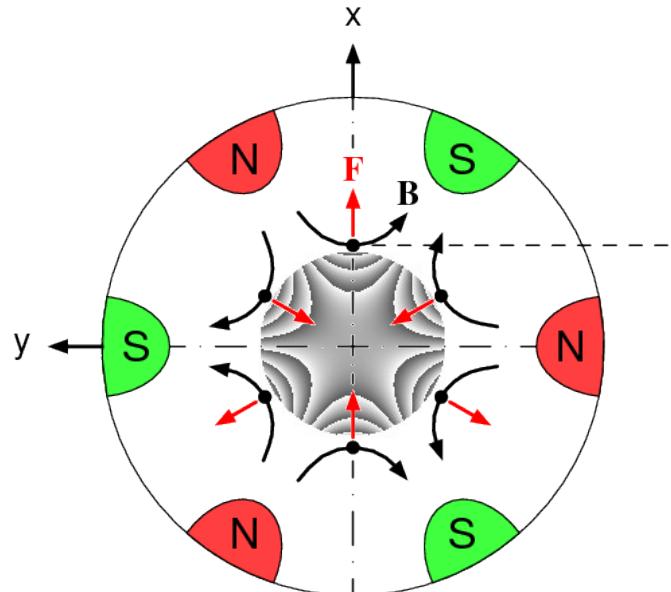
H. Rose

Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG

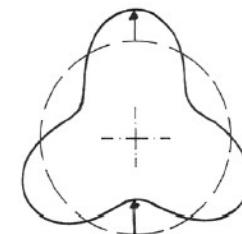
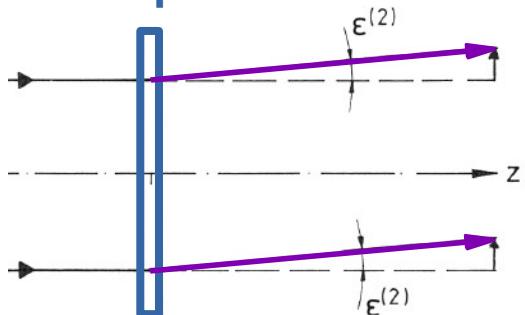




# Aberration correction by means of hexapoles



short  
hexapole

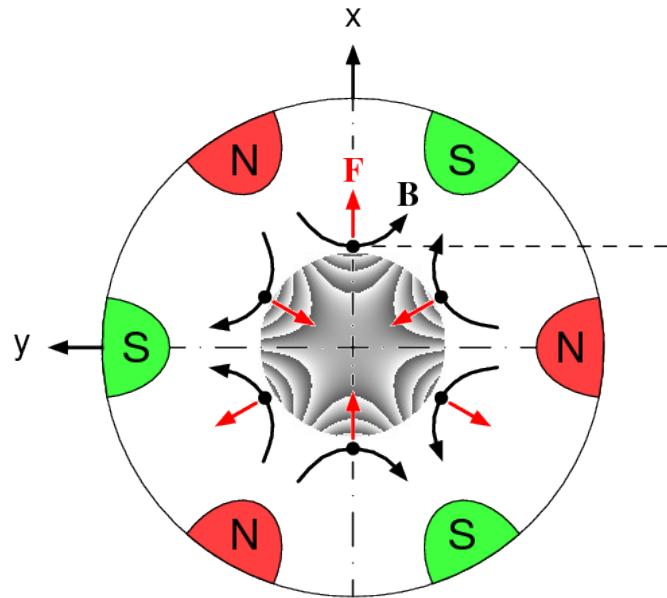


linear

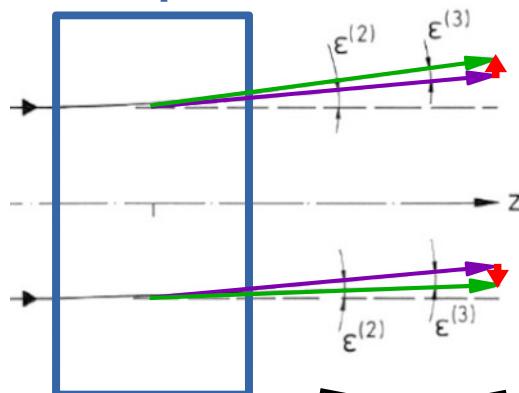
2nd order aberration  
(three-fold astigmatism)



# Aberration correction by means of hexapoles

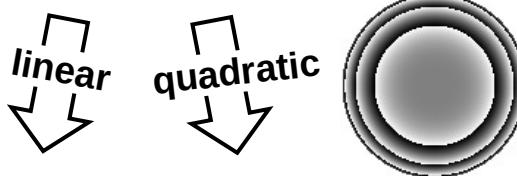


extended  
hexapole



2nd order aberration  
(three-fold astigmatism)

3rd order aberration  
(negative spherical aberration)

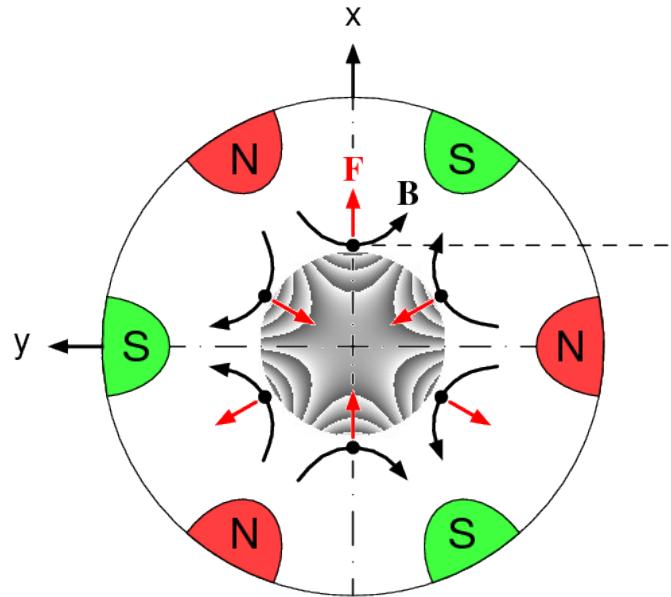


Peter W. Hawkes: "The geometrical aberrations of general electron optical systems",  
Philos. Trans. R. Soc. Lond. A, 257 (1965), 479-552.

Vernon D. Beck: "A hexapole spherical aberration corrector", Optik. 53 (1979), 241–255.



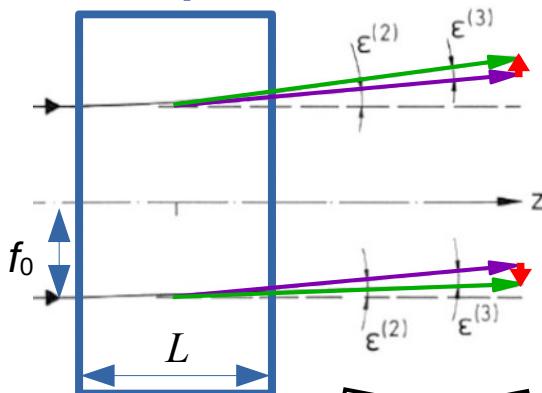
# Aberration correction by means of hexapoles



$\Psi_{3S}$  ... magnetic potential  
 $L$  ... hexapole length  
 $f_0$  ... paraxial ray height

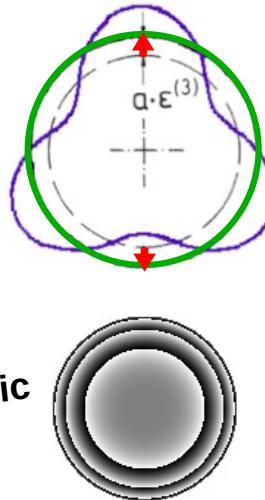
$\eta$  ... constant:  $\eta = \sqrt{\frac{|e|}{2m_0 U_0^*}}$

## extended hexapole



linear

quadratic



2nd order aberration  
(three-fold astigmatism)

$$A_2 = 3 \eta \Psi_{3S} L f_0^3$$

linear

3rd order aberration  
(negative spherical aberration)

$$C_3 = -3 |\eta \Psi_{3S}|^2 L^3 f_0^4 < 0$$

quadratic

M. Haider et al., AIEP Vol. 153 (2008), 43-119, [https://doi.org/10.1016/S1076-5670\(08\)01002-1](https://doi.org/10.1016/S1076-5670(08)01002-1)

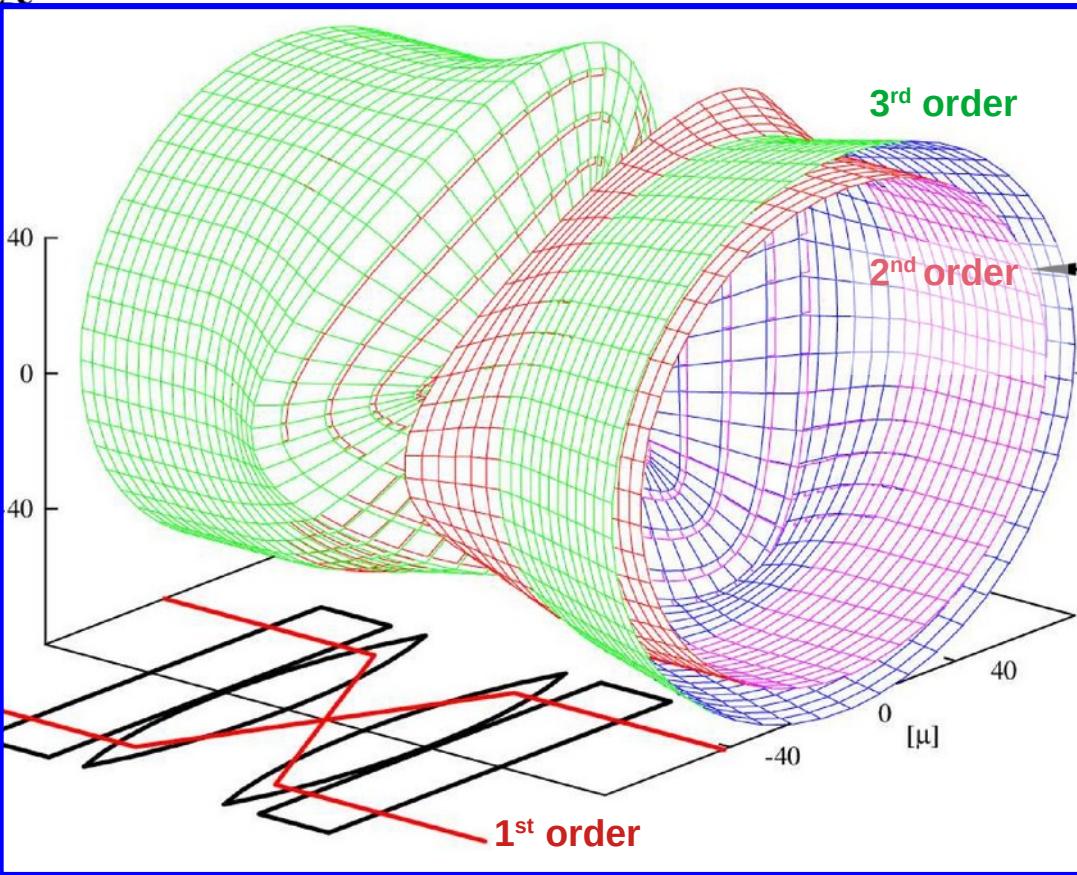
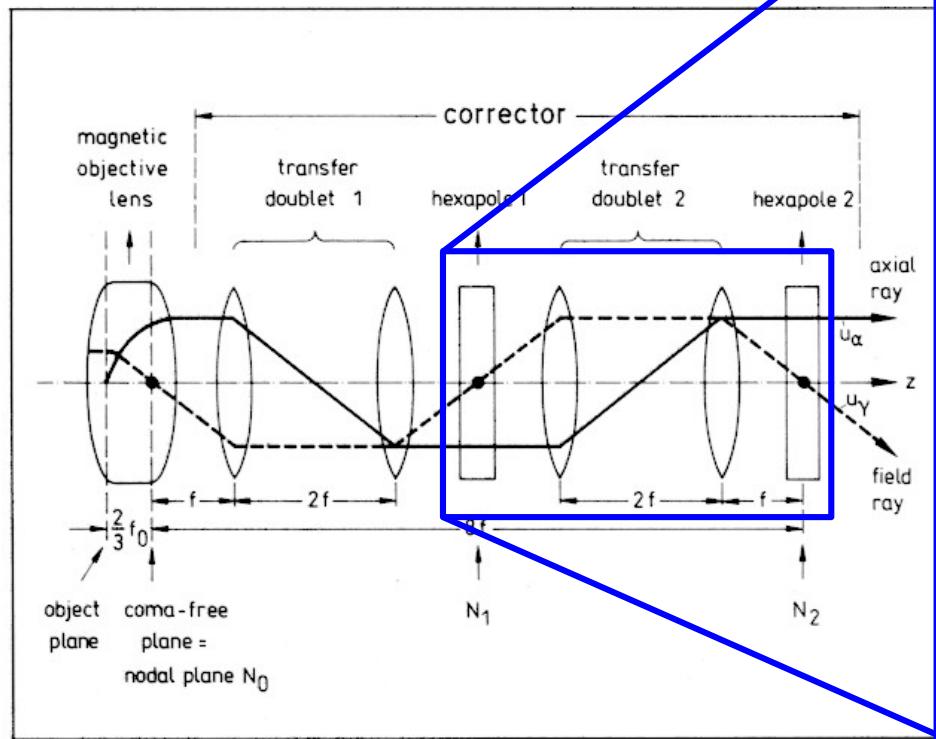


# Aberration correction by means of hexapoles

## Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

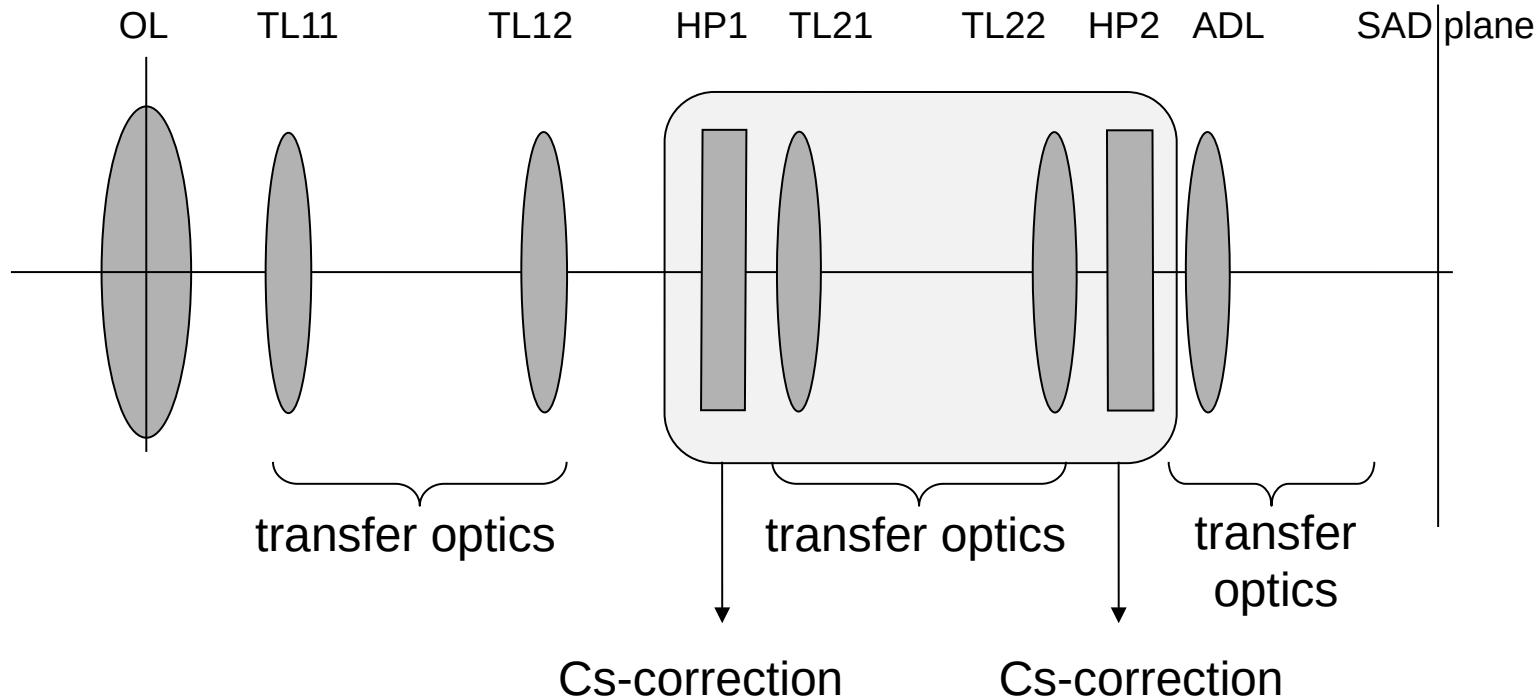
Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG





# Aberration correction by means of hexapoles

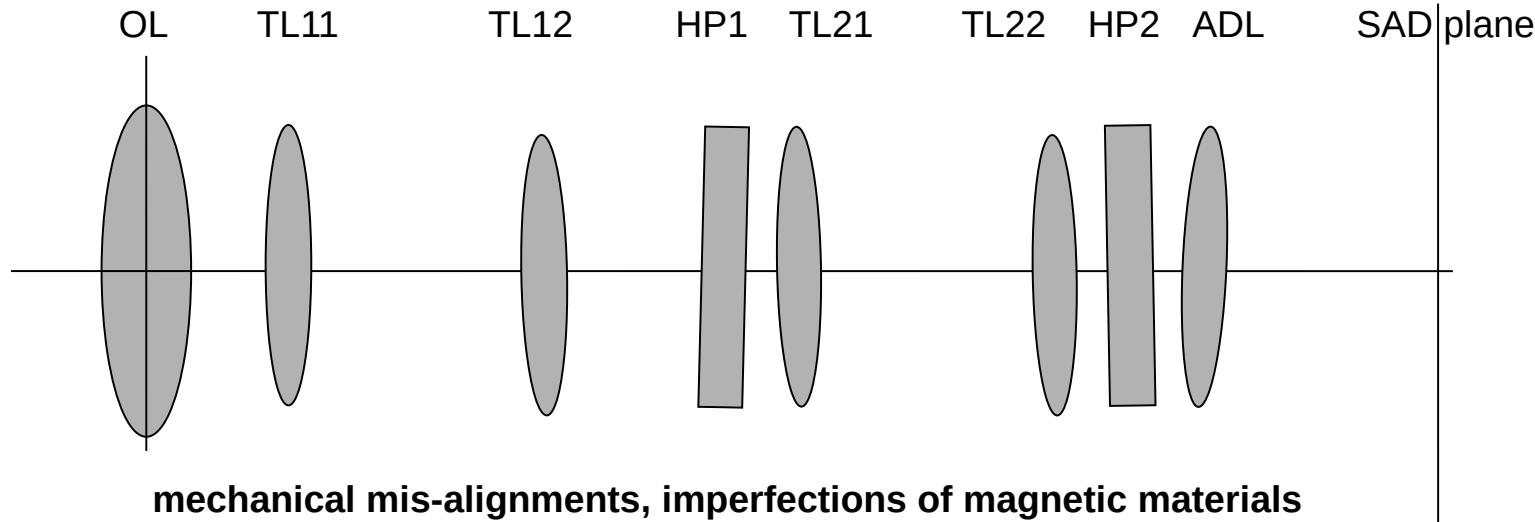
Ideal system:





# Aberration correction by means of hexapoles

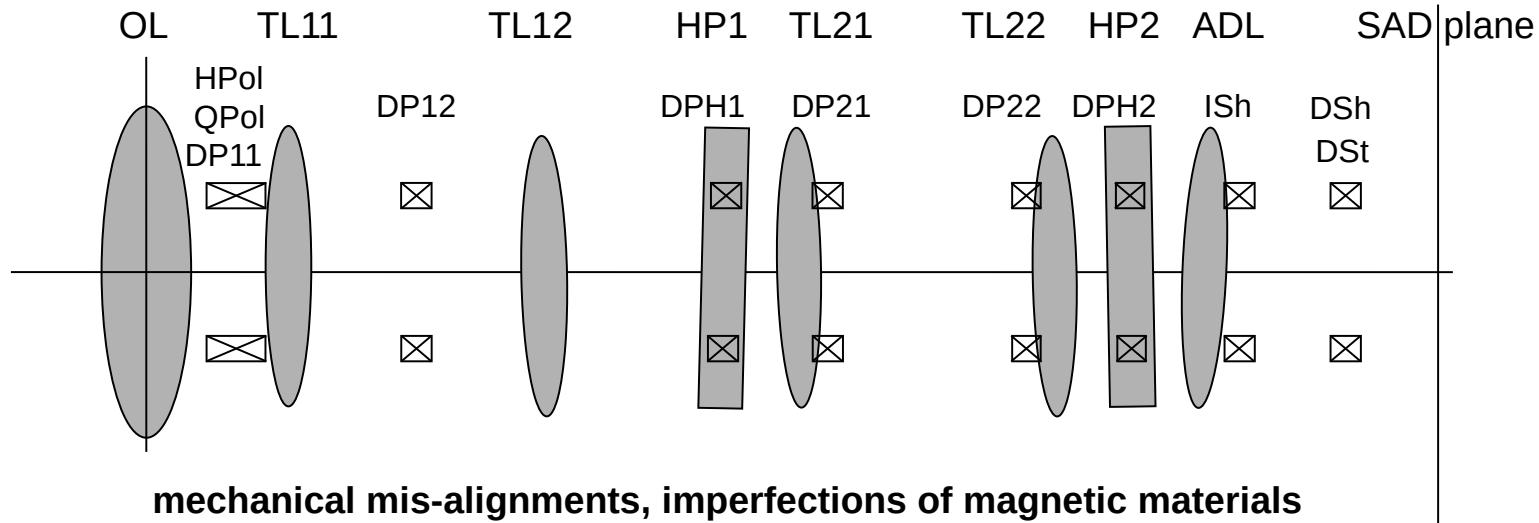
**Ideal system vs. real system:** small imperfections due to limited manufacturing precision





# Aberration correction by means of hexapoles

**Ideal system vs. real system:** small imperfections due to limited manufacturing precision



## Fundamental corrector alignment:

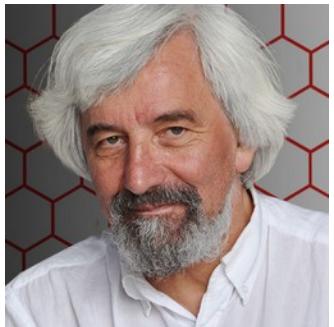
- Factory adjustment = fingerprint of machining tolerances and mechanical mis-alignments
- No change over time! ... *not even when moving a corrector to a different microscope*

## Daily corrector alignment procedure:

- Fine-tuning against hysteresis of magnetic elements and thermal drift.



# 1997: Breakthrough in $C_s$ -correction for TEM



Prof. Max Haider

Electron microscopy  
image enhanced

NATURE | VOL 392 | 23 APRIL 1998

Maximilian Haider\*, Stephan Uhlemann\*,  
Eugen Schwan

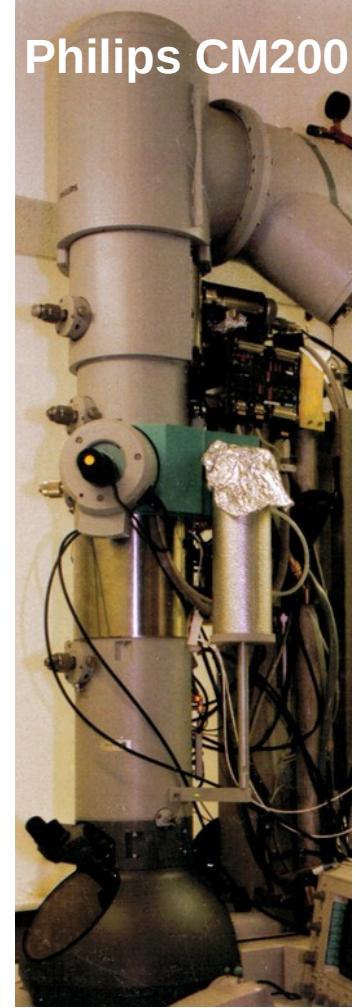
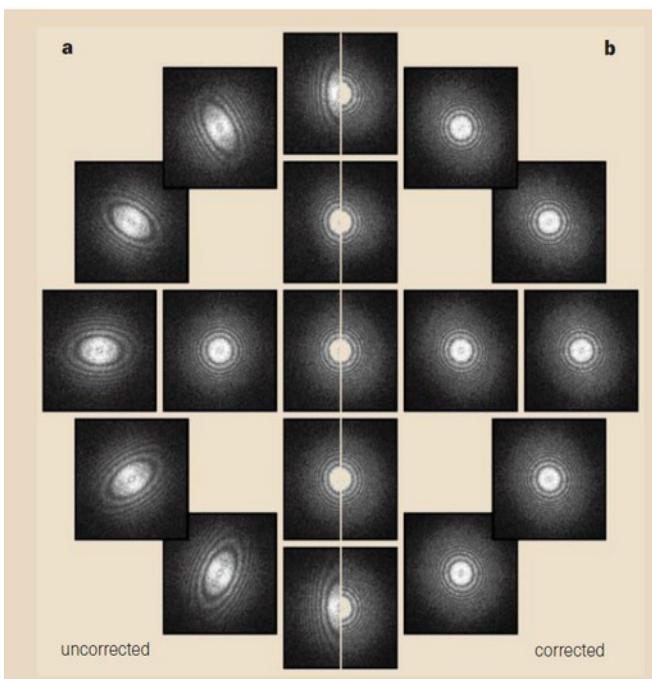
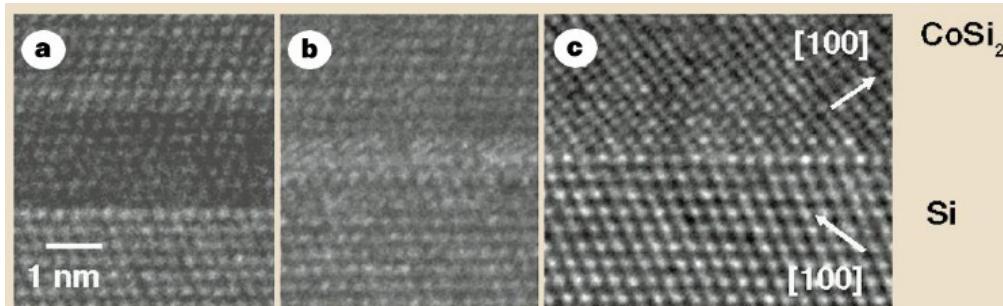
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Feld 519, 69120 Heidelberg, Germany

Harald Rose

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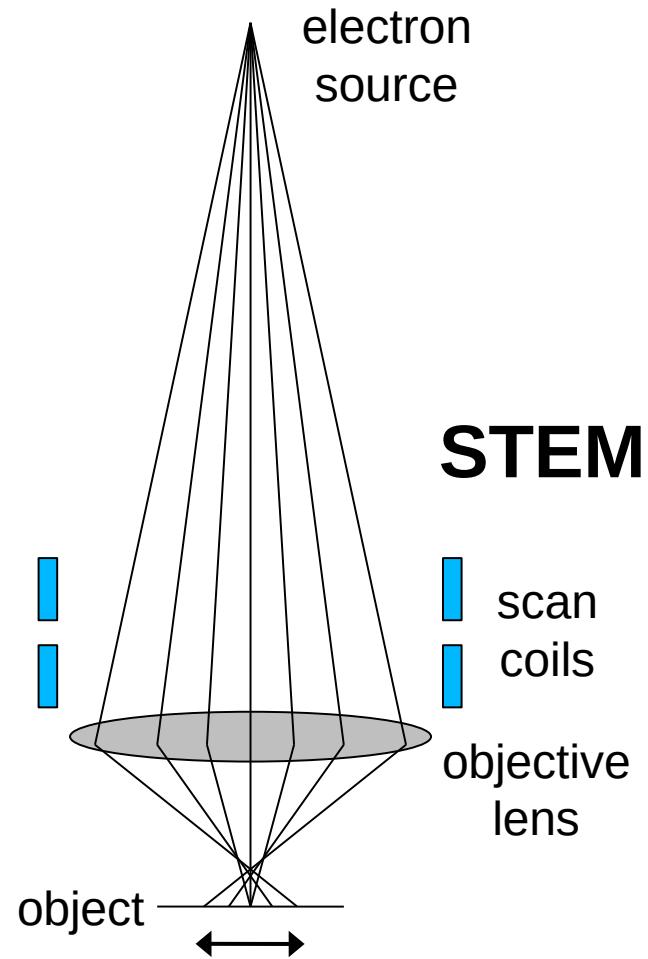
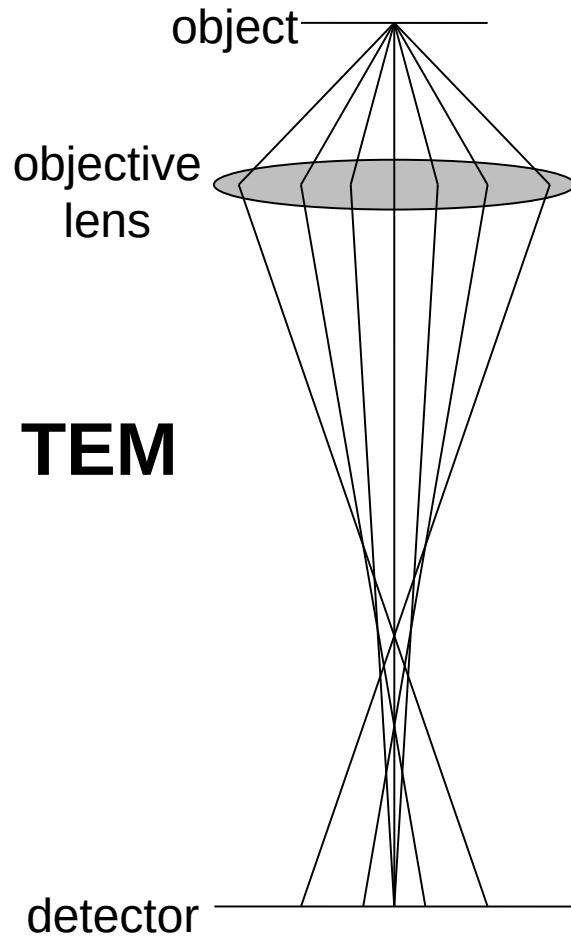
Bernd Kabius, Knut Urban  
*Institut für Festkörperforschung,  
Forschungszentrum Jülich GmbH,  
52425 Jülich, Germany*



Philips CM200

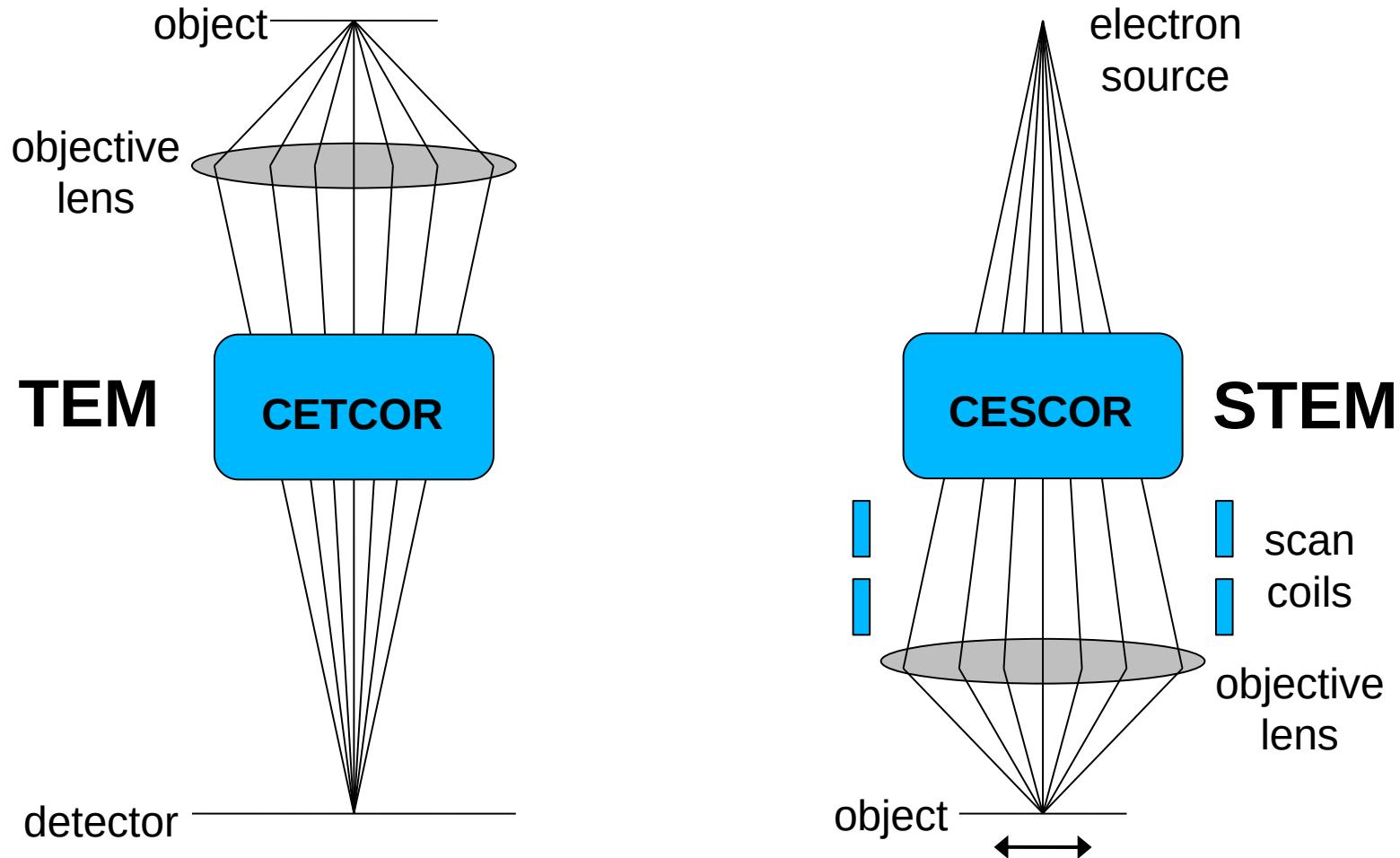


# Aberration-correction for TEM and STEM



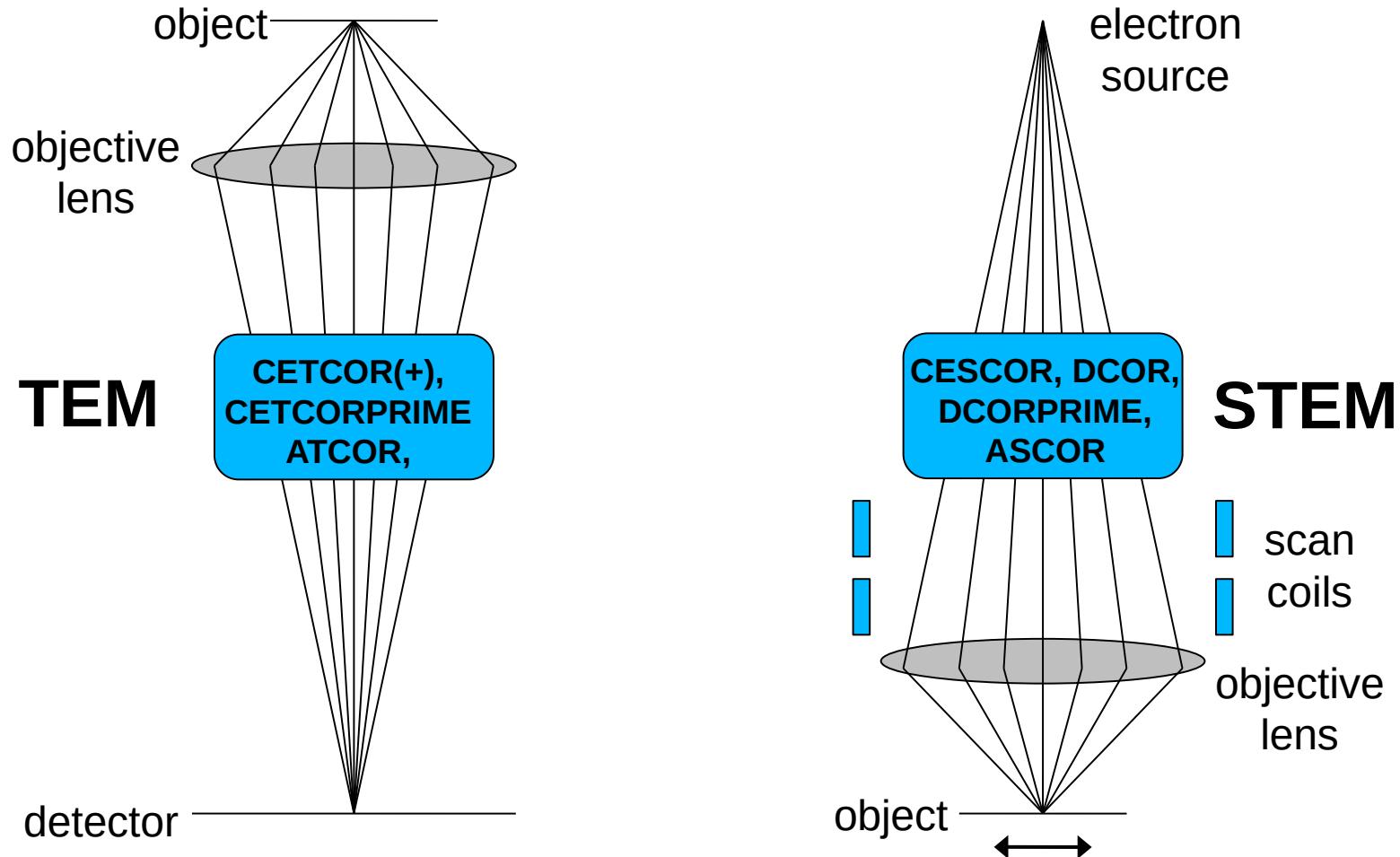


# Aberration-correction for TEM and STEM



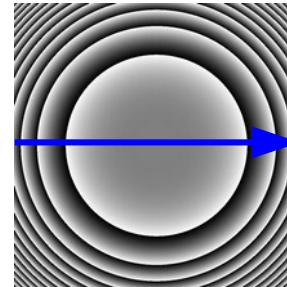
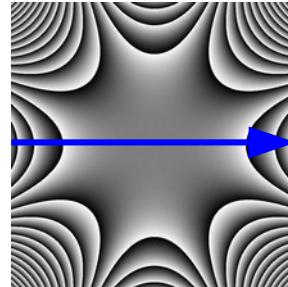


# Aberration-correction for TEM and STEM



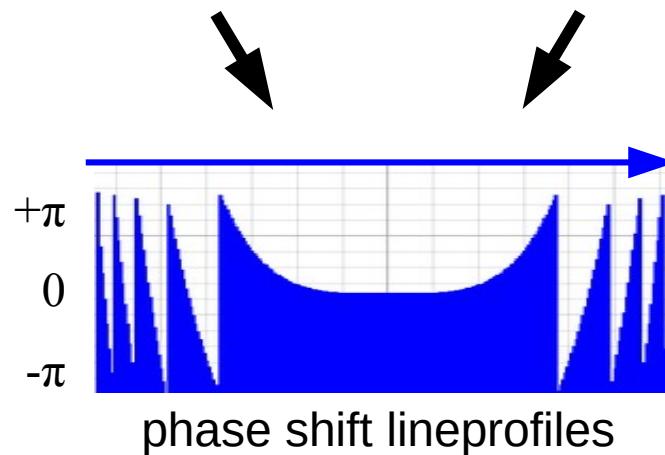
# Aberration correction using quadrupoles and octupoles

# $C_s$ -correction by means of octupoles



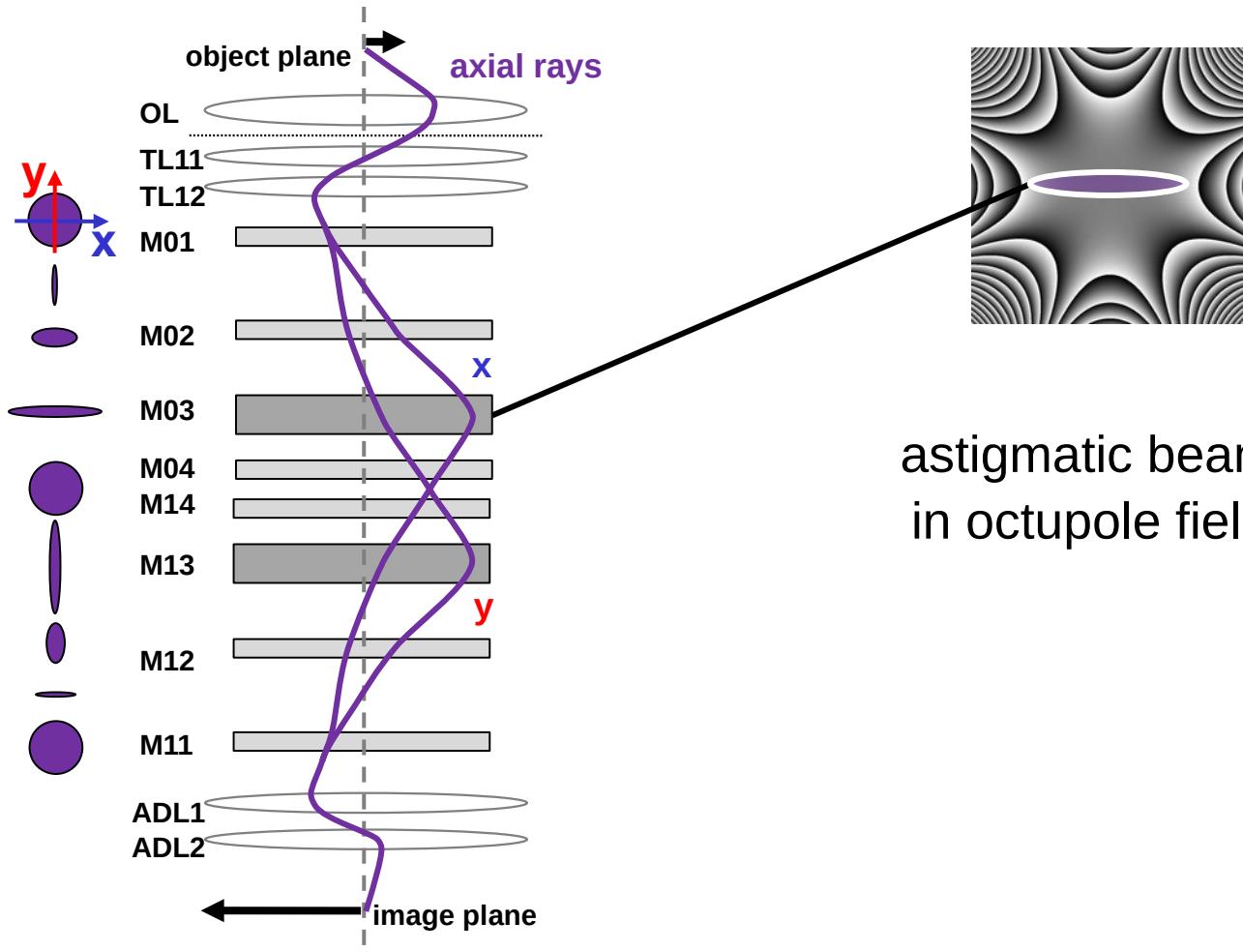
phase shift in  
octupole field

spherical  
aberration





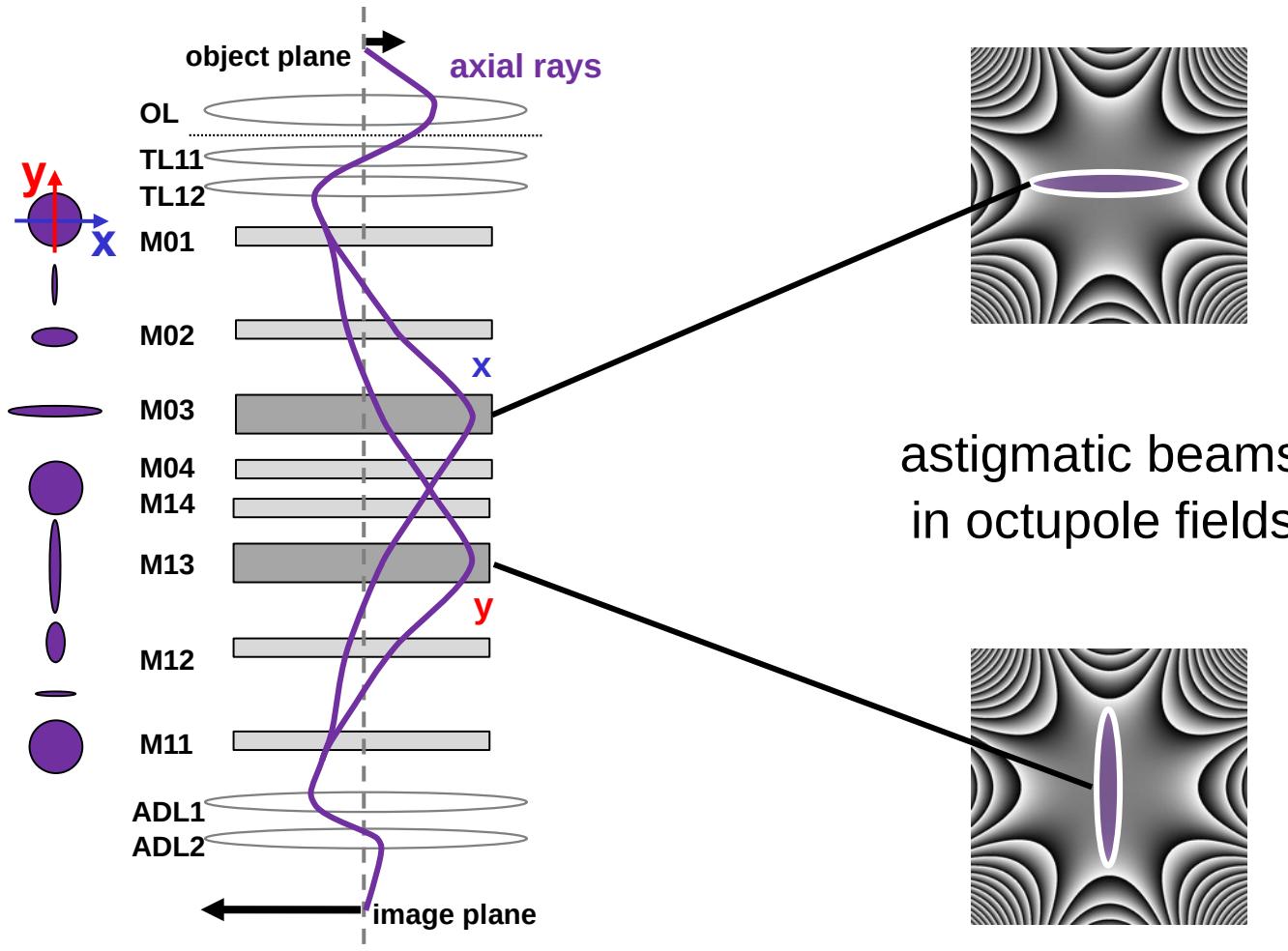
# $C_s$ -correction by means of octupoles



astigmatic beam  
in octupole field



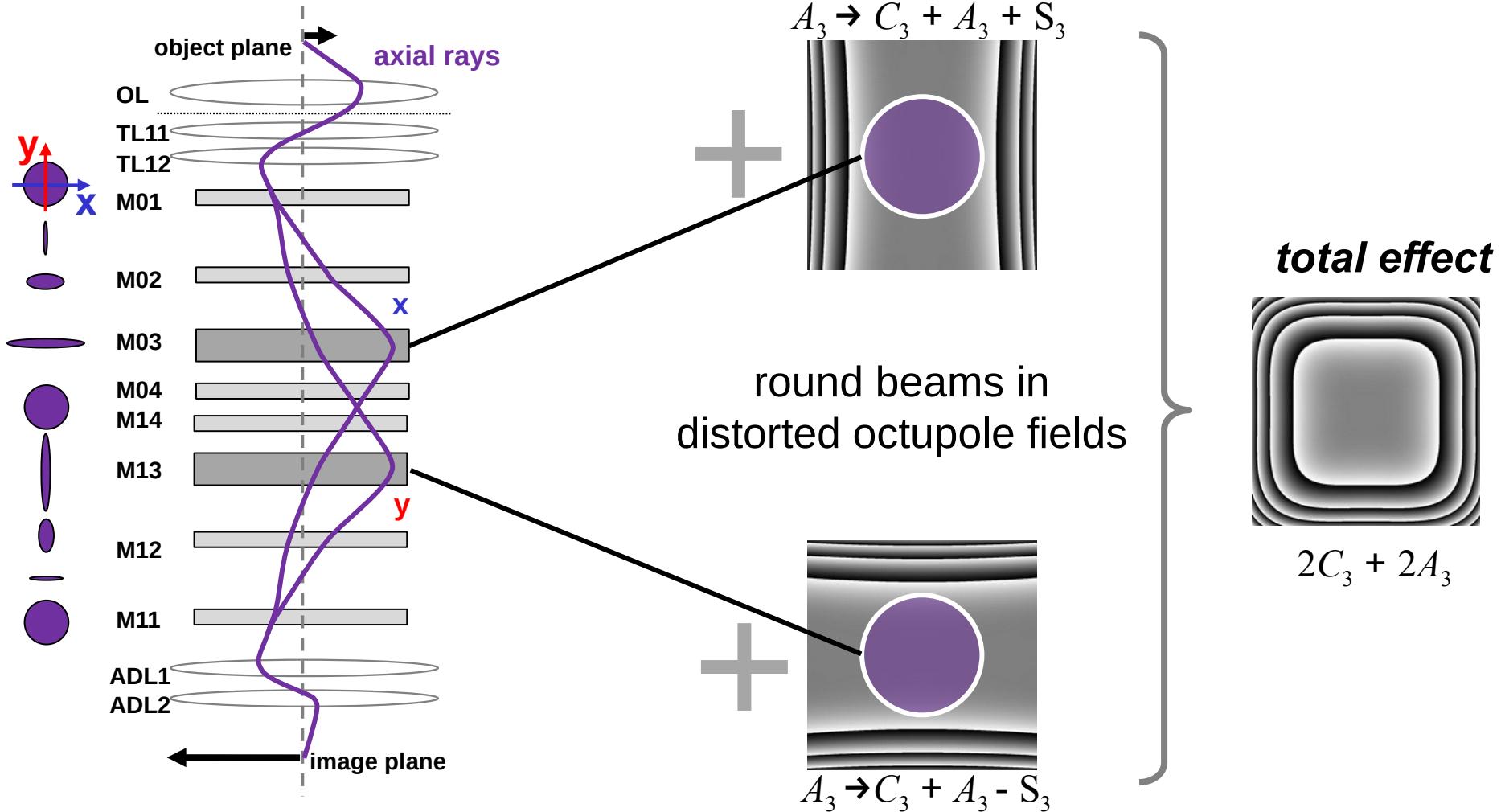
# $C_s$ -correction by means of octupoles



astigmatic beams  
in octupole fields

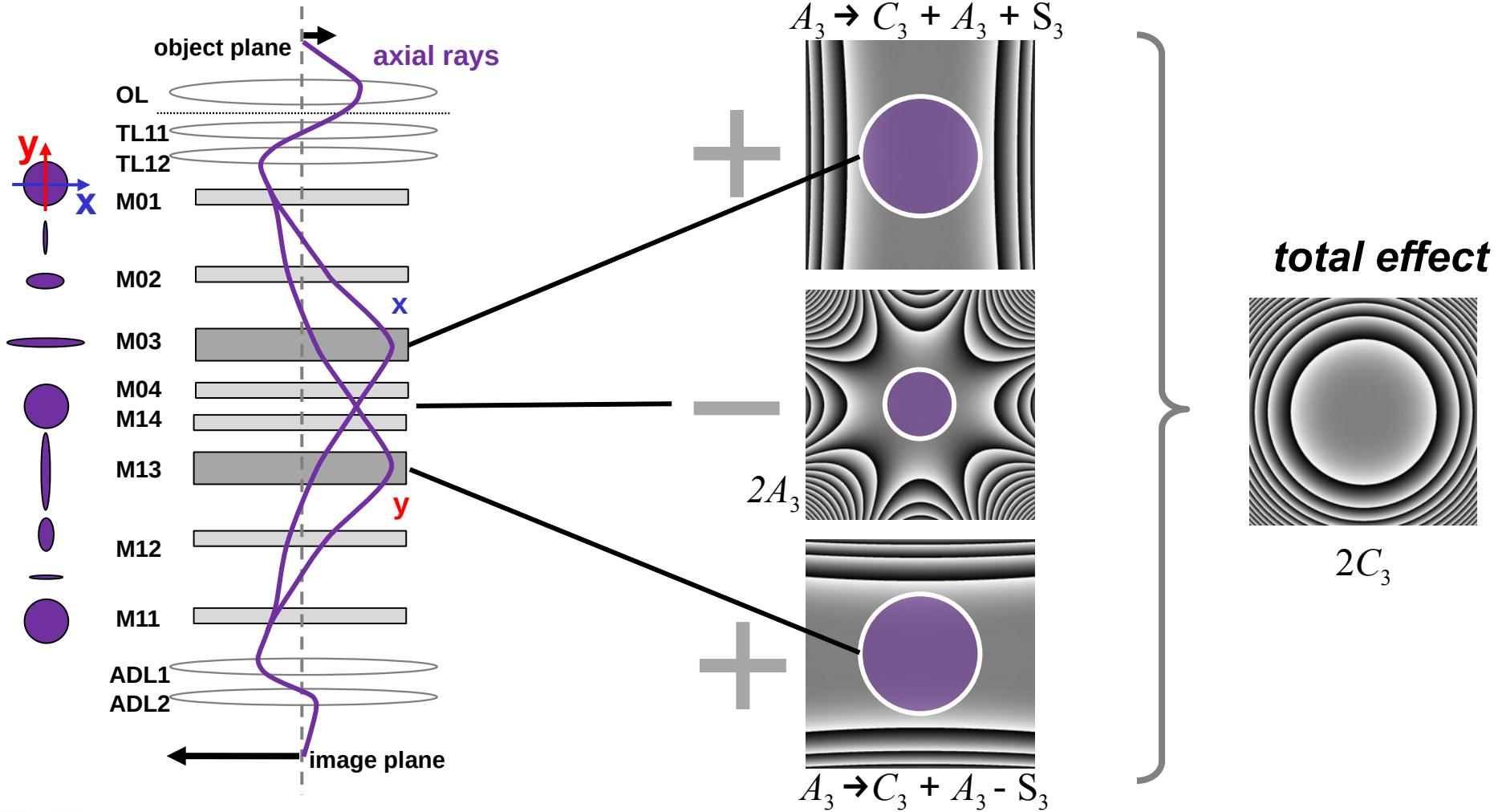


# $C_s$ -correction by means of octupoles





# $C_s$ -correction by means of octupoles

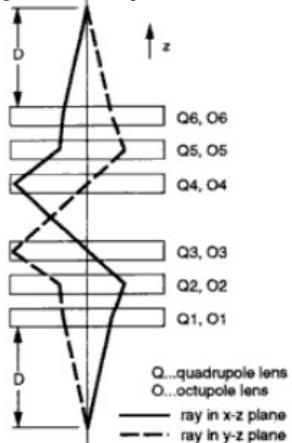




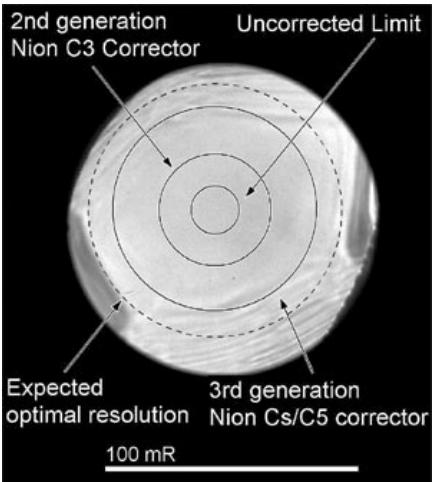
Niklas Dellby and Ondrey Krivanek



- Resolution improvement by Cs-correction in a VG HB5 STEM (1997) based on a 1964 concept from J. Deltrap, Cavendish labs (UK)
- Today: complete nion STEM column with monochromator and spectrometer



from: Krivanek et al. Inst. Phys.  
Conf. Ser. 153 (Proc. 1997 EMAG)



<http://www.nion.com>

Nion UltraSTEM 100

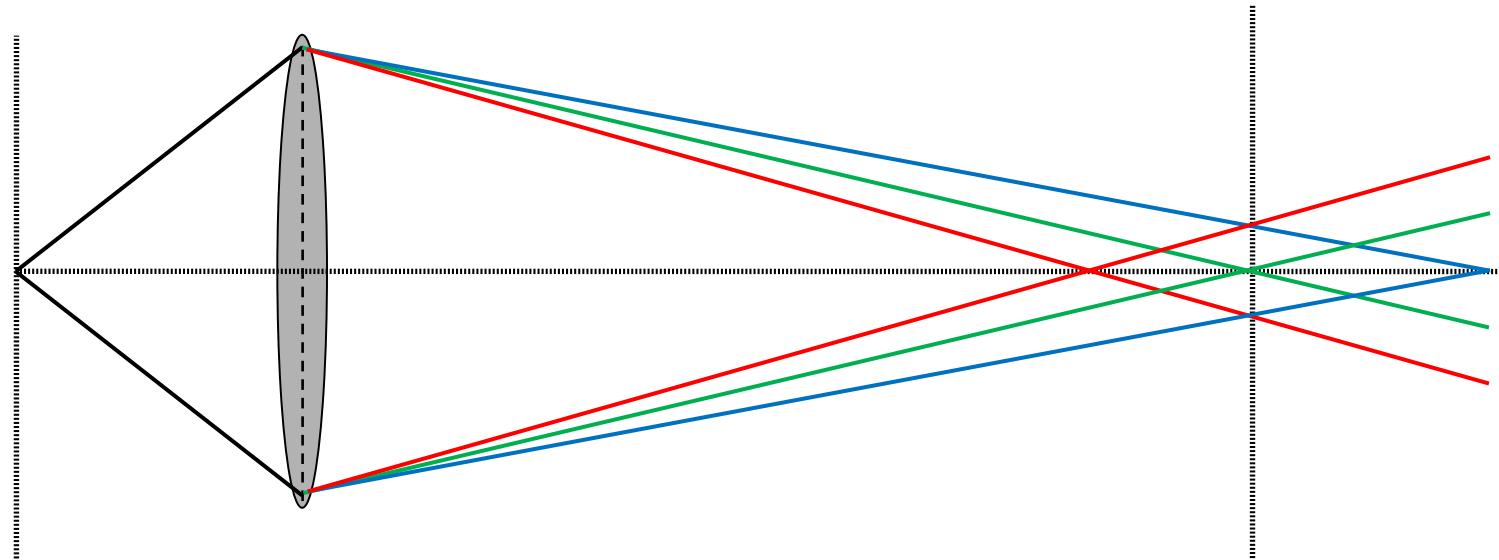


<http://www.nion.com>



# Chromatic aberration

Electron energy:  $E_0 - \Delta E < E_0 < E_0 + \Delta E$



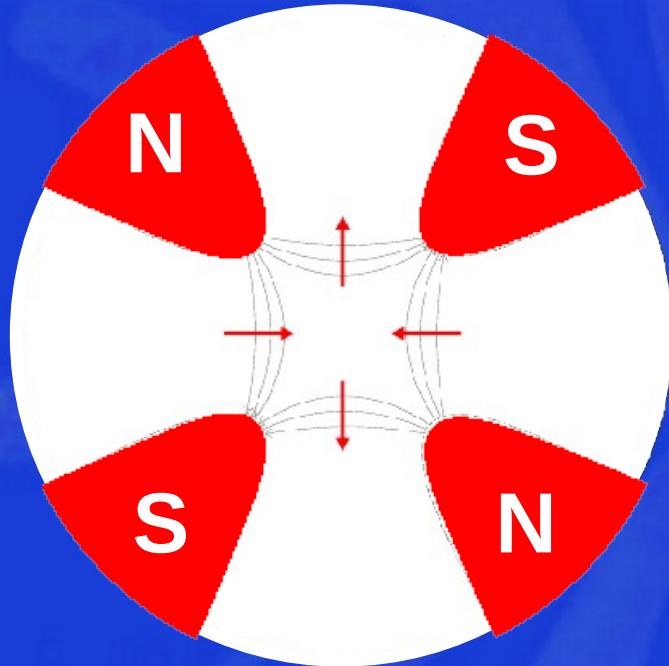
Object  
plane

Gaussian  
image plane

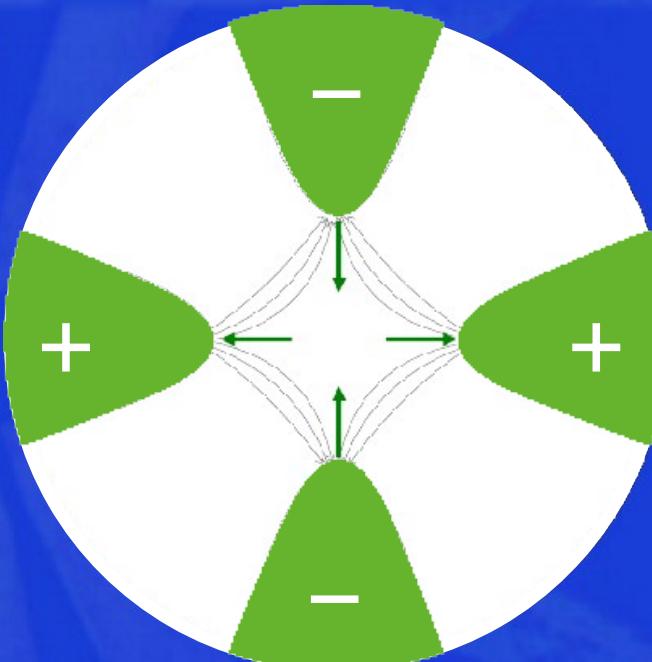


# Chromatic aberration correction

magnetic QP



electric QP



$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$



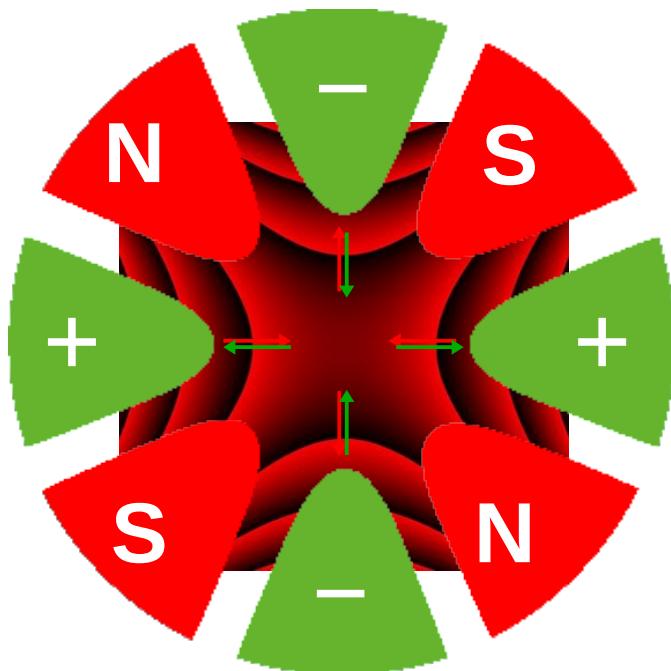


# Chromatic aberration correction

## Crossed electric and magnetic fields:

equation of motion

$$\frac{d}{dt}(\vec{m}\vec{v}) = -e(\vec{E} + \vec{v} \times \vec{B})$$



Wien filter:  $= 0$   
for exact energy  $E_0$

$E < E_0$ : quadrupole effect

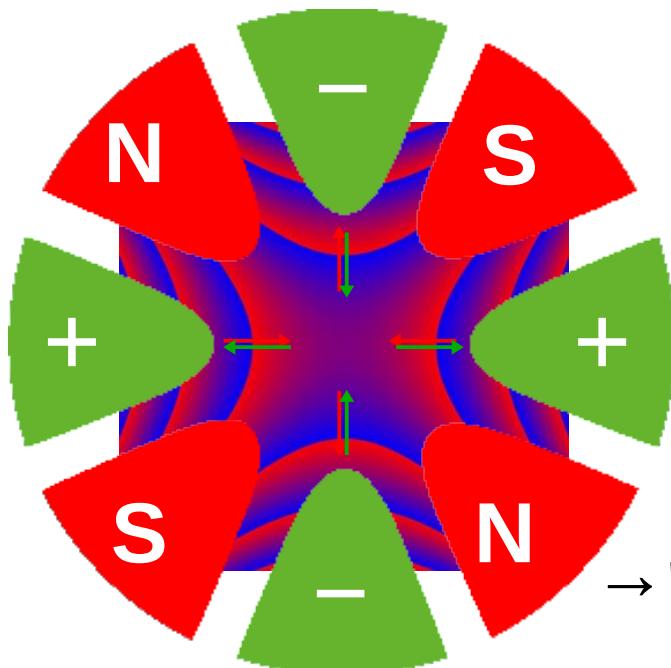


# Chromatic aberration correction

## Crossed electric and magnetic fields:

equation of motion

$$\frac{d}{dt}(\vec{m}\vec{v}) = -e(\vec{E} + \vec{v} \times \vec{B})$$



Wien filter:  $= 0$   
for exact energy  $E_0$

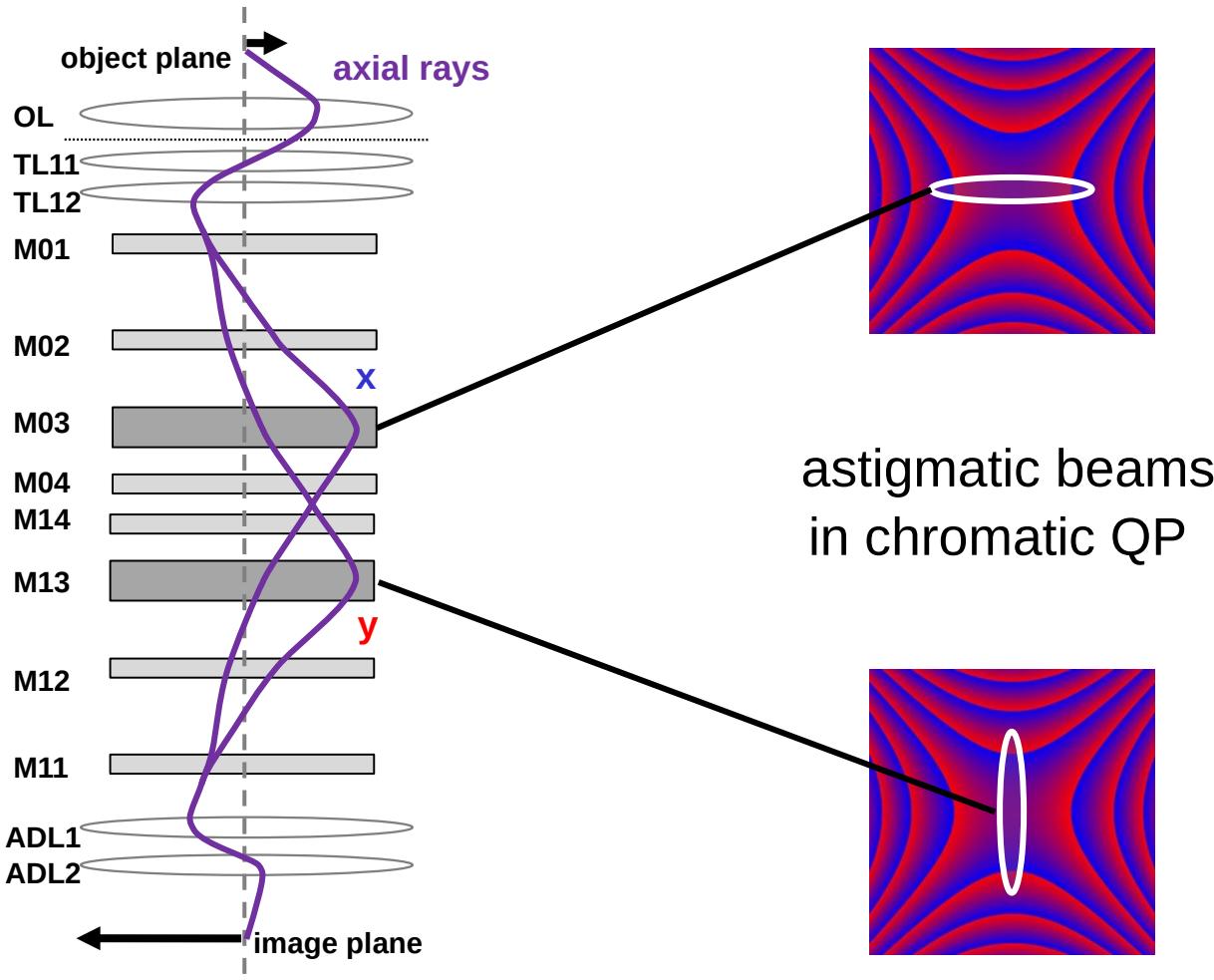
$E < E_0$ : quadrupole effect

$E > E_0$ : opposite QP effect

→ "chromatic quadrupole"  $A_{1c}$



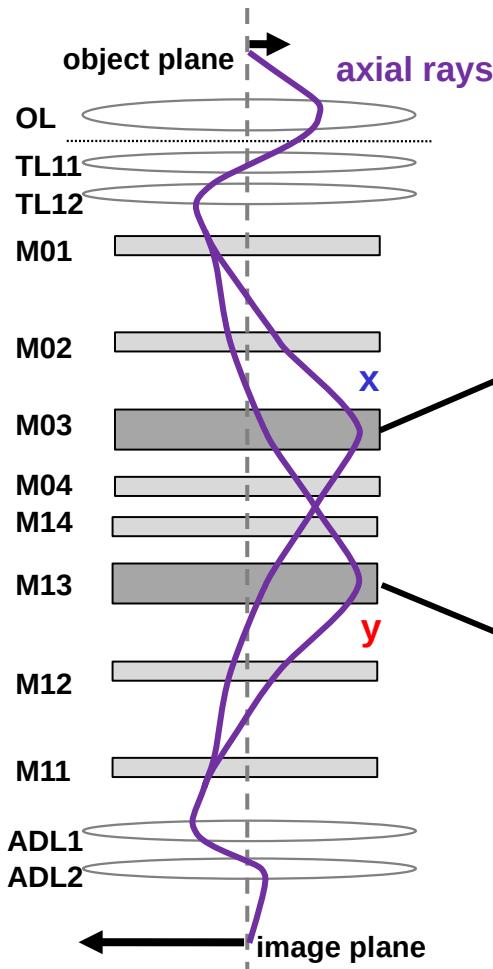
# Chromatic aberration correction



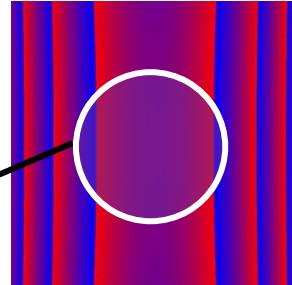
astigmatic beams  
in chromatic QP



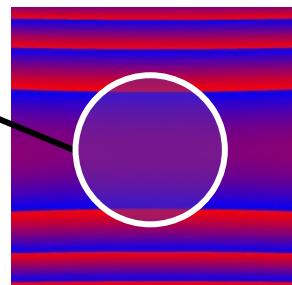
# Chromatic aberration correction



$$A_{1c} \rightarrow A_{1c} + C_{1c}$$

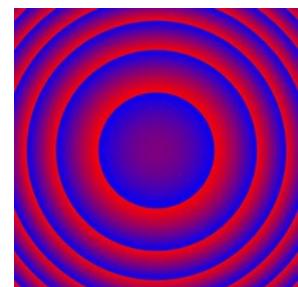


round beams in  
distorted chromatic QP



$$A_{1c} \rightarrow A_{1c} - C_{1c}$$

**total effect**



$$-2C_{1c}$$



1995: First ever working and resolution improving corrector

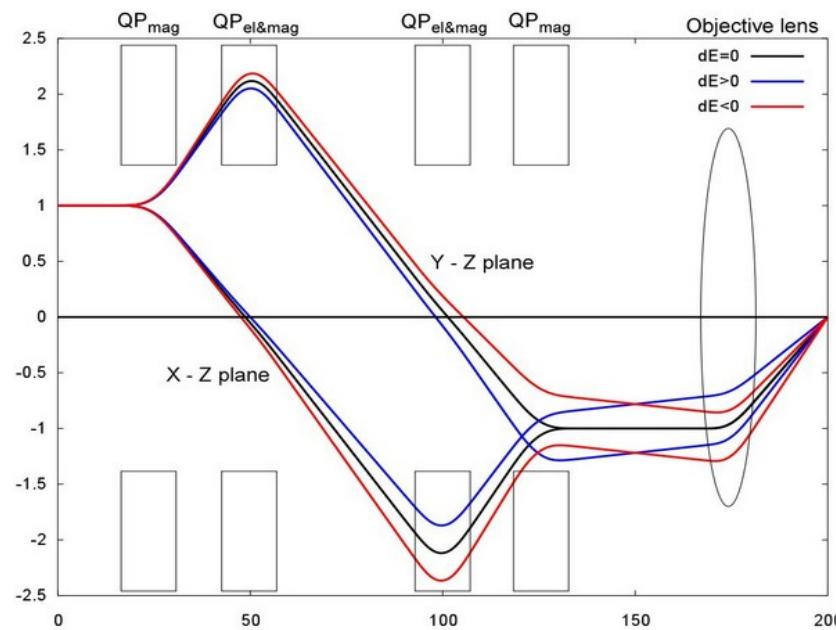
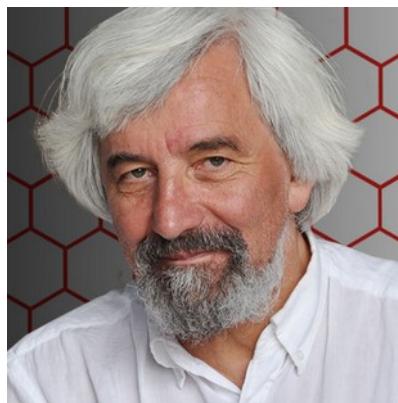
Optik

98, No. 3 (1995) 112–118

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## Correction of spherical and chromatic aberration in a low voltage SEM

J. Zach, M. Haider





1995: First ever working and resolution improving corrector

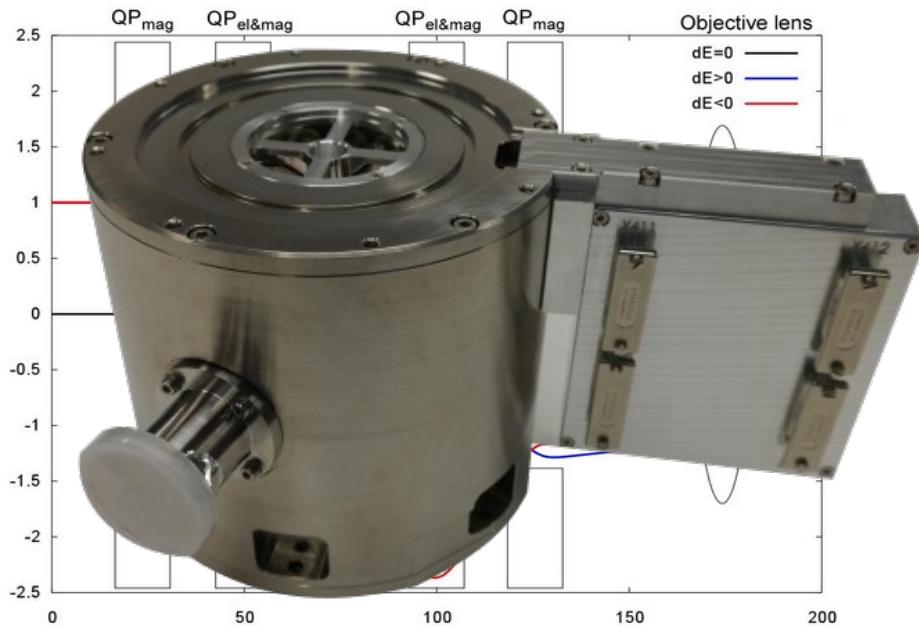
Optik

98, No. 3 (1995) 112–118

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## Correction of spherical and chromatic aberration in a low voltage SEM

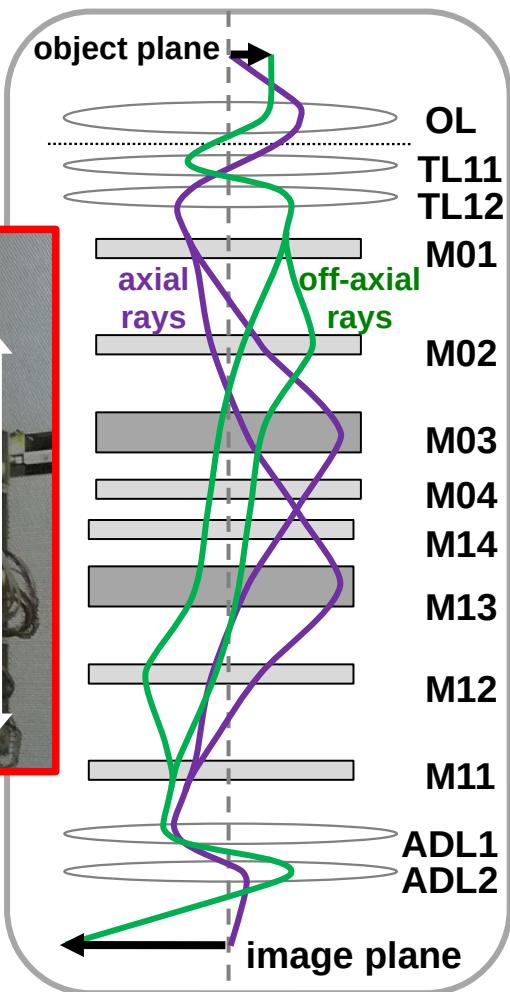
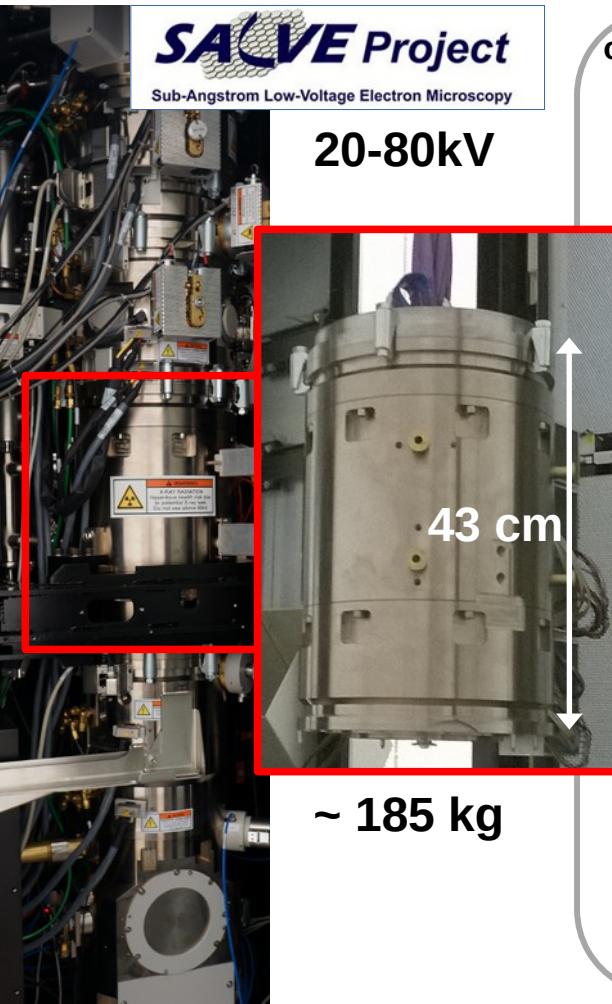
J. Zach, M. Haider





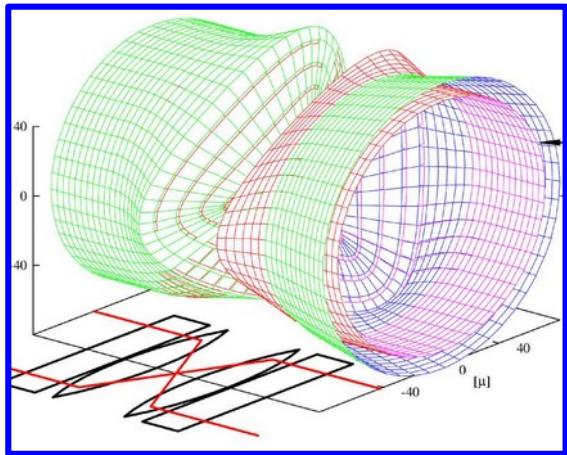
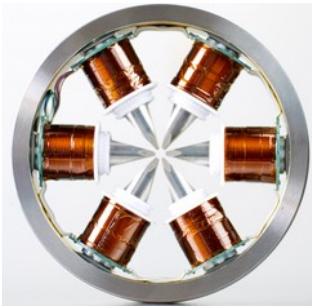
# $C_c$ - and $C_s$ -correction for TEM

CCOR 30-300kV 160 channels

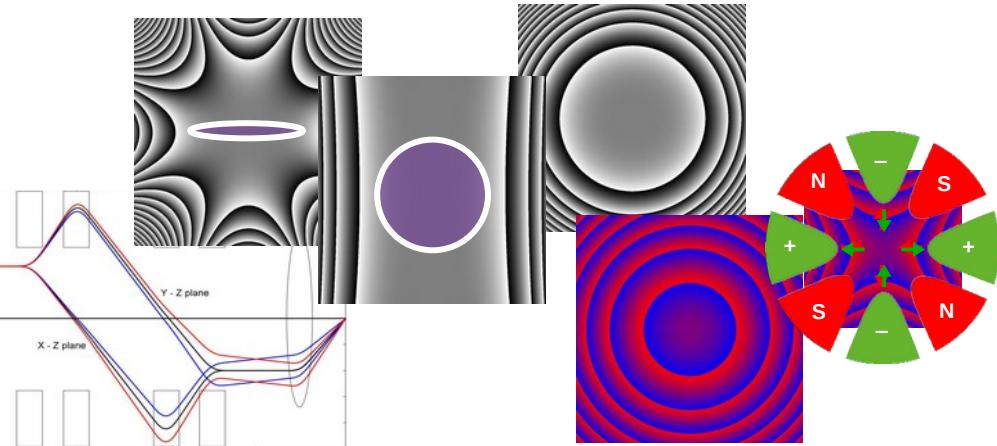




## $C_s$ -correction with hexapoles



## $C_C$ - $C_S$ -correction with quadrupoles and octupoles



## Further resources

R. Erni: "Aberration-Corrected Imagingin TEM" (second edition 2015).

P.W. Hawkes: "The correction of electron lens aberrations", Ultramicroscopy 156 (2015), A1-A64.

M. Haider et al.: "Present and Future Hexapole Aberration Correctors for High-Resolution Electron Microscopy", Advances in Imaging and Electron Physics, Volume 153, 43-119, ISSN 1076-5670.

H. Müller et al.: "Aberration-corrected optics: from an idea to a device", Physics Physics Procedia 1 (2008), 167–178.